



# Integration of Plug-In Electric Vehicles in Renewable-Dominated Power Systems

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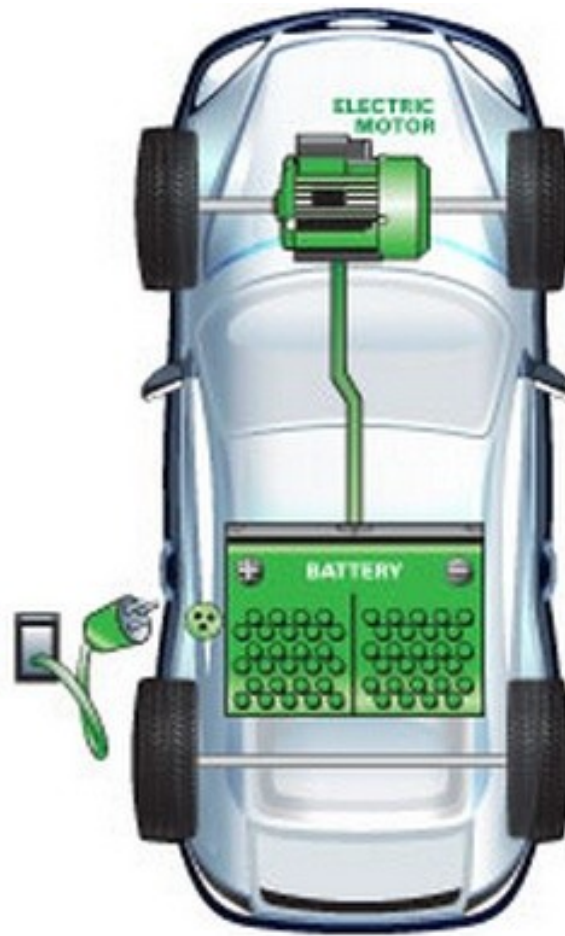
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# Motivation

- It is expected a high increment of the number of PEVs



# Plug-in Electric Vehicles



# Drawbacks of using Electrical Vehicles



- Consumers acceptance (uncertainty)
- Reduced autonomy
- Small diversity of electrical vehicles (nowadays)
- Technological evolution (uncertainty)
- Need of charging point at home
- Reduced number of outdoor charging points
- High purchase cost

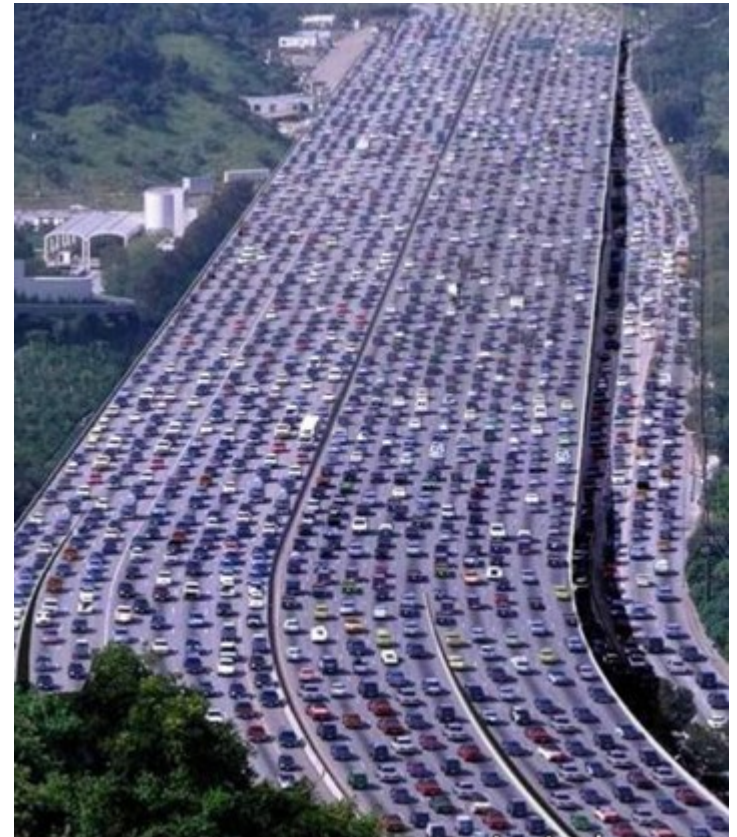
# Advantages of Using Electrical Vehicles



- Increase of the energetic independence
- Reduction of the effects of the environmental issue (reduction of contaminant emissions)
- Increase of the energetic efficiency (well to wheel)
- Reduction of noise pollution

# Impact in Power Systems

- A large increment in the number of electrical vehicles:
  - Is it affordable by a power system?
  - What are the consequences? (electricity prices, CO<sub>2</sub> emissions, generating mix,...)



# Plug-in Electric Vehicles (EVs) in power systems

## □ Active research topic

- W. Kempton, S. E. Letendre, 1997
- J. Tomic, W. Kempton, 2007
- H. Lund and W. Kempton, 2008
- C. K. Ekman, 2011
- D. Dallinger and M. Wietshel, 2011
- M. A. Ortega, F. Bouffard and V. Silva, 2013
- K. Seddig, P. Jochem and W. Fitchner, 2014

# Objective

- Analysis of the incorporation of a significant number of EVs in a power system with a large penetration of renewable energy
  - Controlled/Uncontrolled charge of EVs
  - Stochastic dispatch model



# PEVs modeling

- ❑ PEVs are equipped with a **large battery** that is charged from the grid
- ❑ Definition of several **groups of PEVs** with similar behavior patterns
- ❑ The **time interval** in which PEVs can be charged is defined for each group
- ❑ **Initial battery status** of each group is estimated (daily distance driven, consumption per km, etc.)

# Charge modeling

## □ Uncontrolled charge

- Charging process is not controlled by the ISO

## □ Grid-to-vehicle control (G2V)

- Charging process is controlled by the ISO

## □ Vehicle-to-grid control (V2G)

- Charging and discharging processes are controlled by the ISO

# Stochastic dispatch model

- Stochastic dispatch model that co-optimizes simultaneously energy and reserve

(Pritchard et al., 2010, Morales et al., 2012, Domínguez et al., 2014)

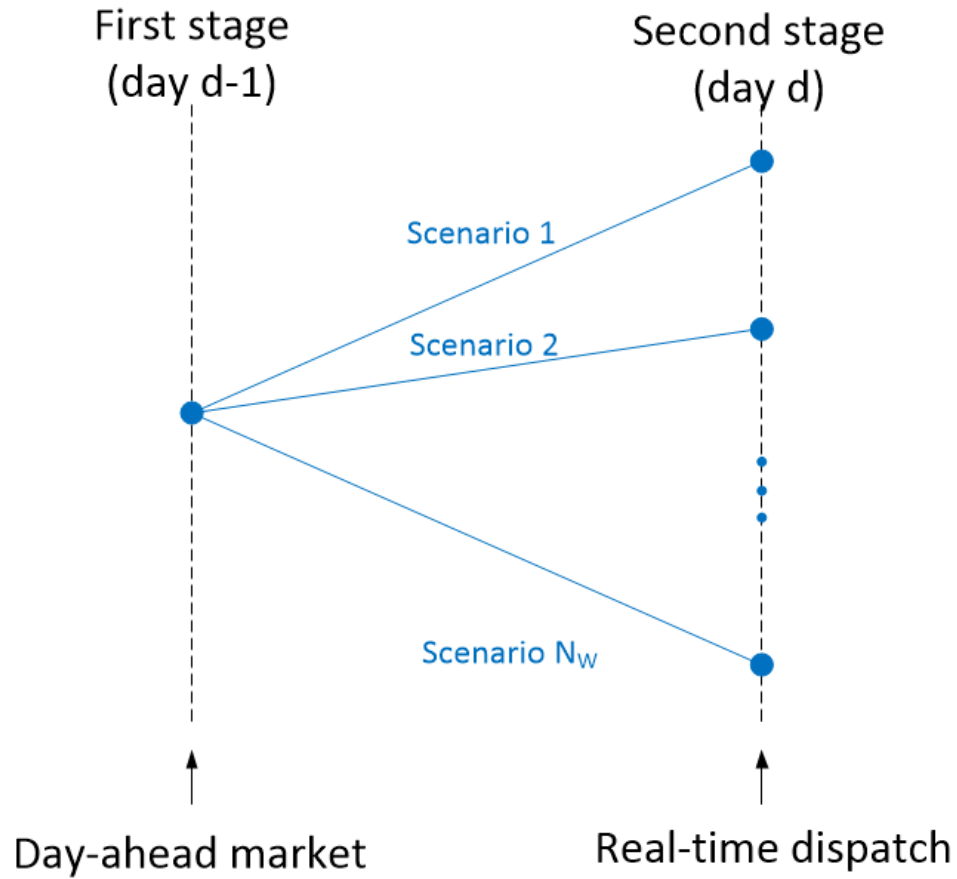
- Energy scheduling (Day-ahead schedule)
  - Pool prices
- Real-time operation (Real-time dispatch)
  - Balancing prices

# Decision stages

## □ Two-stage stochastic programming model

- First stage:
  - Energy schedule
  - Uncontrolled charge of PEVs (additional inelastic load)
- Second stage:
  - Reserve deployment (changes in the energy schedule)
  - Controlled charge/discharge of PEVs (decided by ISO)
    - Charge: Down reserve
    - Discharge: Up reserve

# Decision framework



# Model assumptions

- Smart grid framework
- Inelastic loads
- Linear generating-side offers
- Minimum power outputs equal to zero
- DC model of the transmission network
- Reserve capacity bids are not considered
- Equipment failures are not considered

# Uncertainty

## □ Uncertain parameters

- Demand
- Renewable resources (wind, PV)
- PEV demand

## □ Modelled using a set of scenarios

# Optimization problem

Minimize Expected generation costs

Subject to:

- Technical constraints

- Reserve deployment constraints

- Power flow constraints

  - Power balance on day-ahead schedule

- Power balance for deviations in the real-time dispatch

  - State-of-charge of PEVs



# Objective function

Minimize<sub>Θ</sub>

Day-ahead energy costs

$$\sum_{t \in S^T} \left( \sum_{c \in S^C} C_c^{\text{CO}} p_{ct}^{\text{C,Disp}} + \sum_{h \in S^H} C_h^{\text{HO}} p_{ht}^{\text{H,Disp}} \right)$$

$$+ \sum_{\omega \in S^\Omega} \pi_\omega \sum_{t \in S^T} \left( \sum_{c \in S^C} C_c^{\text{CO}} (r_{ct\omega}^{\text{CDu}} - r_{ct\omega}^{\text{CDd}}) + \sum_{h \in S^H} C_h^{\text{HO}} (r_{ht\omega}^{\text{HDu}} - r_{ht\omega}^{\text{HDd}}) \right)$$

$$+ \sum_{n \in N} C_n^{\text{UD}} p_{ntw}^{\text{UD}}$$

Reserve deployment  
energy costs

Load shedding costs

# Technical constraints

$$0 \leq p_{ctw}^C \leq P_{\max,c}^C, \quad \forall c \in S^C, \forall t \in S^T, \forall \omega \in S^\Omega$$

$$p_{ctw}^C - p_{ct-1,\omega}^C \leq P_{\text{up},c}^C, \quad \forall c \in S^C, \forall t \in S^T, \forall \omega \in S^\Omega$$

$$p_{ct-1,\omega}^C - p_{ct,\omega}^C \leq P_{\text{down},c}^C, \quad \forall c \in S^C, \forall t \in S^T, \forall \omega \in S^\Omega$$

Thermal units

$$0 \leq p_{htw}^H \leq P_{\max,h}^H, \quad \forall h \in S^H, \forall t \in S^T, \forall \omega \in S^\Omega$$

Hydro units

$$p_{rtw}^R + p_{rtw}^{RS} = U_{rtw}^R P_{\max,r}^R, \quad \forall r \in S^R, \forall t \in S^T, \forall \omega \in S^\Omega$$

Renewable units

$$p_{rtw}^R, p_{rtw}^{RS} \geq 0, \quad \forall r \in S^R, \forall t \in S^T, \forall \omega \in S^\Omega$$

# Reserve constraints

$$0 \leq r_{ct\omega}^{\text{CDu}} \leq R_{ct}^{\text{CSu}}, \quad \forall c \in S^{\text{C}}, \forall t \in S^{\text{T}}, \forall \omega \in S^{\Omega}$$

$$0 \leq r_{ct\omega}^{\text{CDd}} \leq R_{ct}^{\text{CSd}}, \quad \forall c \in S^{\text{C}}, \forall t \in S^{\text{T}}, \forall \omega \in S^{\Omega}$$

$$p_{ct\omega}^{\text{C}} = p_{ct}^{\text{C,Disp}} + r_{ct\omega}^{\text{CDu}} - r_{ct\omega}^{\text{CDd}}, \quad \forall c \in S^{\text{C}}, \forall t \in S^{\text{T}}, \forall \omega \in S^{\Omega}$$

Thermal units

$$0 \leq r_{ht\omega}^{\text{HDu}} \leq R_{ht}^{\text{HSu}}, \quad \forall h \in S^{\text{H}}, \forall t \in S^{\text{T}}, \forall \omega \in S^{\Omega}$$

$$0 \leq r_{ht\omega}^{\text{HDd}} \leq R_{ht}^{\text{HSd}}, \quad \forall h \in S^{\text{H}}, \forall t \in S^{\text{T}}, \forall \omega \in S^{\Omega}$$

$$p_{ht\omega}^{\text{H}} = p_{ht}^{\text{H,Disp}} + r_{ht\omega}^{\text{HDu}} - r_{ht\omega}^{\text{HDd}}, \quad \forall c \in S^{\text{H}}, \forall t \in S^{\text{T}}, \forall \omega \in S^{\Omega}$$

Hydro units

# Power flows

$$p_{ltw}^L = \frac{1}{X_\ell} (\theta_{O(\ell)tw} - \theta_{F(\ell)tw}), \quad \forall \ell \in S^L, \forall t \in S^T, \forall \omega \in S^\Omega$$

$$-P_{\max,\ell}^L \leq p_{ltw}^L \leq P_{\max,\ell}^L, \quad \forall \ell \in S^L, \forall t \in S^T, \forall \omega \in S^\Omega$$

$$-\pi/2 \leq \theta_{ntw} \leq \pi/2, \quad \forall n \in S^N, \forall t \in S^T, \forall \omega \in S^\Omega$$

# Power balance on day-ahead schedule

$$\begin{aligned}
 \sum_{c \in S_n^C} p_{ct}^{C, \text{Disp}} + \sum_{h \in S_n^H} p_{ht}^{H, \text{Disp}} + \sum_{r \in S_n^R} p_{rt}^{R, \text{Disp}} - \sum_{\ell \in S_{O,n}^L} p_{\ell t}^{L, \text{Disp}} + \sum_{\ell \in S_{F,n}^L} p_{\ell t}^{L, \text{Disp}} = \\
 = P_{nt}^{D, \text{Exp}} + \sum_{k \in S_n^K} (1 - \gamma_{kn}^{\text{EV}}) P_{knt}^{\text{EV}, \text{Exp}} (\lambda_{nt})
 \end{aligned}$$

$\forall n \in S^N, \forall t \in S^T$

# Power balance for deviations in the real-time dispatch

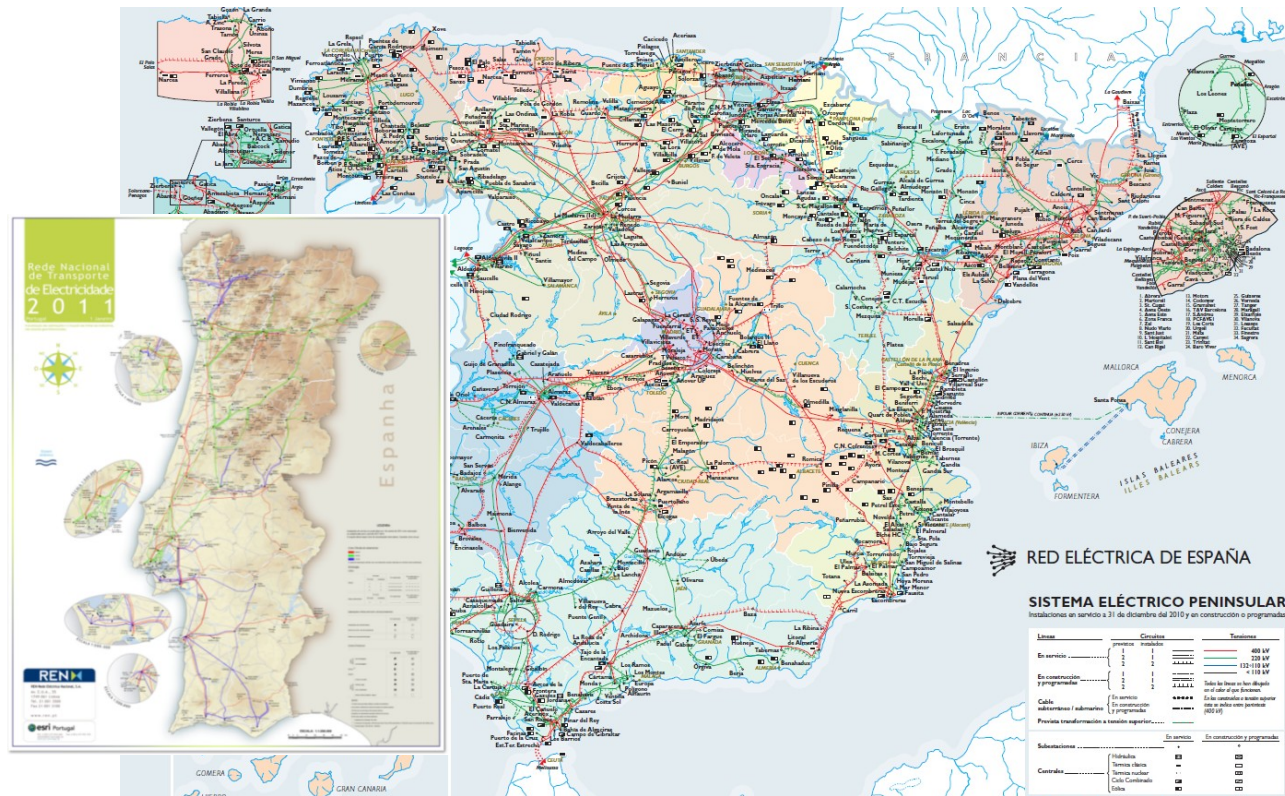
$$\begin{aligned}
 & \sum_{c \in S_n^C} (r_{ctw}^{CDu} - r_{ctw}^{CDd}) + \sum_{h \in S_n^H} (r_{htw}^{HDu} - r_{htw}^{HDd}) + \sum_{r \in S_n^R} (p_{rtw}^R - p_{rt}^{R,Disp}) \\
 & - \sum_{\ell \in S_{O,n}^L} (p_{ltw}^L - p_{lt}^{L,Disp}) + \sum_{\ell \in S_{F,n}^L} (p_{ltw}^L - p_{lt}^{L,Disp}) + p_{ntw}^{UD} = \\
 & = P_{ntw}^D - P_{nt}^{D,Exp} + \sum_{k \in S_n^K} (1 - \gamma_{kn}^{EV}) (P_{kntw}^{EV} - P_{knt}^{EV,Exp}) \\
 & + \left[ \sum_{k \in S_n^K} p_{kntw}^{BC} - \sum_{k \in S_n^K} p_{kntw}^{BD} \right] (\lambda_{ntw}^B) \\
 & \forall n \in S^N, \forall t \in S^T, \forall \omega \in S^\Omega
 \end{aligned}$$

# State-of-charge constraints

$$\begin{aligned}
 p_{knt\omega}^{\text{BS}} &= \gamma_{kn}^{\text{EV}} P_{knd\omega}^{\text{BS},0} N_{kn}^{\text{EV}}, & \forall k, \forall n, t = t_{kd}^{\text{O}} - 1, \forall d, \forall \omega \\
 p_{knt\omega}^{\text{BS}} &= p_{knt-1,\omega}^{\text{BS}} + \alpha_k^{\text{BC}} p_{knt\omega}^{\text{BC}} - \frac{1}{\alpha_k^{\text{BD}}} p_{knt\omega}^{\text{BD}}, & \forall k, \forall n, t = t_{kd}^{\text{O}}, \dots, t_{kd}^{\text{F}}, \forall d, \forall \omega \\
 0 &\leq p_{knt\omega}^{\text{BC}} \leq \gamma_{kn}^{\text{EV}} P_{\text{max}}^{\text{BPT}} N_{kn}^{\text{EV}}, & \forall k, \forall n, t = t_{kd}^{\text{O}}, \dots, t_{kd}^{\text{F}}, \forall d, \forall \omega \\
 0 &\leq \frac{1}{\alpha_k^{\text{BD}}} p_{knt\omega}^{\text{BD}} \leq p_{knt\omega}^{\text{BS}}, & \forall k, \forall n, t = t_{kd}^{\text{O}}, \dots, t_{kd}^{\text{F}}, \forall d, \forall \omega \\
 0 &\leq p_{knt\omega}^{\text{BD}} \leq \gamma_{kn}^{\text{EV}} P_{\text{max}}^{\text{BPT}} N_{kn}^{\text{EV}}, & \forall k, \forall n, t = t_{kd}^{\text{O}}, \dots, t_{kd}^{\text{F}}, \forall d, \forall \omega \\
 p_{knt\omega}^{\text{BS}} &= \gamma_{kn}^{\text{EV}} P_{\text{max},k}^{\text{BS}} N_{kn}^{\text{EV}}, & \forall k, \forall n, t = t_{kd}^{\text{F}}, \forall d, \forall \omega
 \end{aligned}$$

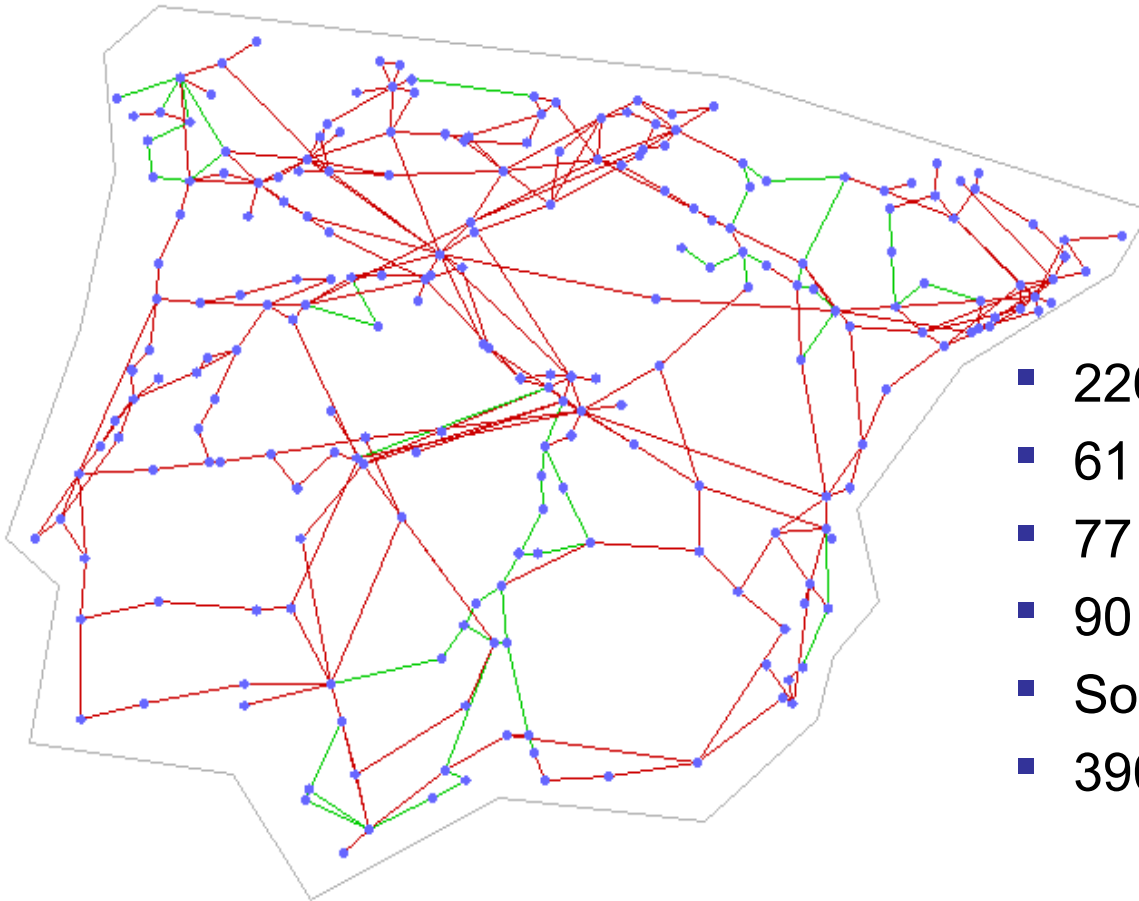
# Case study

## □ Iberian Power System (MIBEL)





# Input data

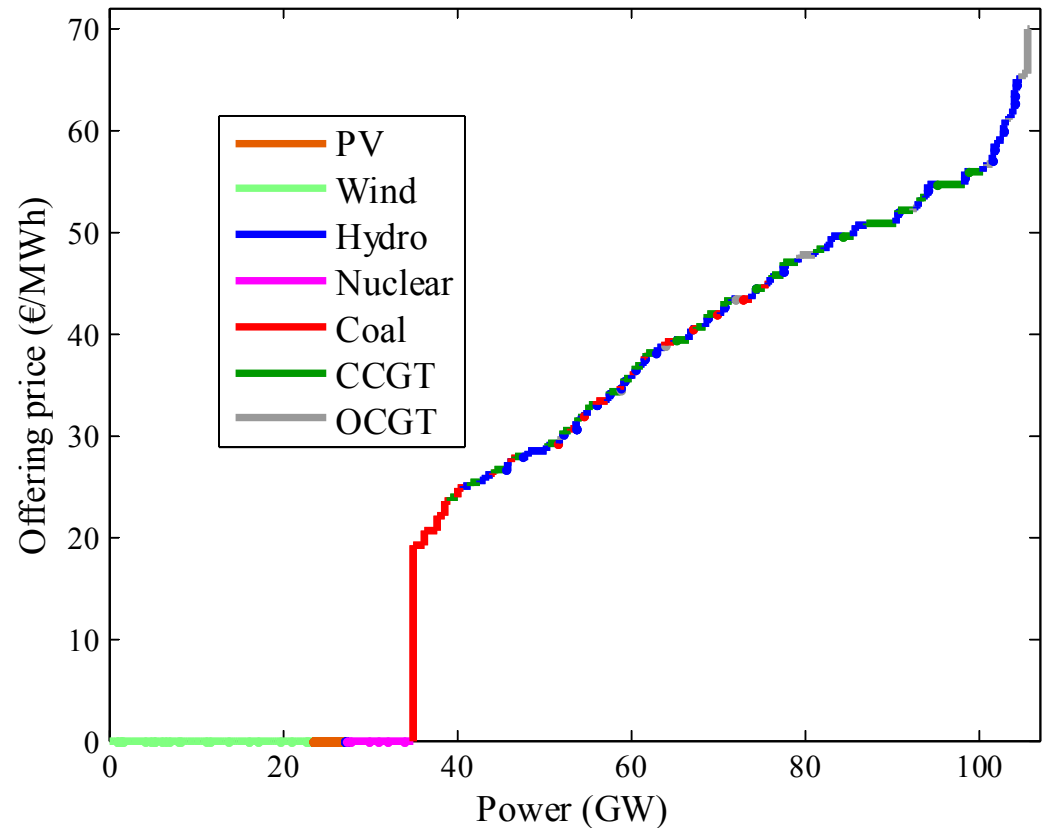


- 226 buses
- 61 conventional generating units
- 77 hydro units
- 90 wind units
- Solar PV distributed per node
- 390 transmission lines

Transmission system based on the equivalent of the European System  
(Zhou and Bialek, 2005)

# Input data

Technology	Capacity (GW)
Nuclear	7.655
Coal	12.519
Gas	5.532
Combined Cycle	31.914
Hydro	21.077
Wind	23.456
PV	3.677
<b>Total</b>	<b>105.830</b>



# Input data

## □ PEVs demand

- Battery capacity: 22 kWh
- Efficiency of charging/discharging: 0.88
- Consumption: 0.18 kW/km
- Charge rate: 7.2 kW (SAE J1772 low)
- Number of vehicles: 30 millions
  - Percentage of PEVs: 30 %

# Input data

## □ PEVs demand

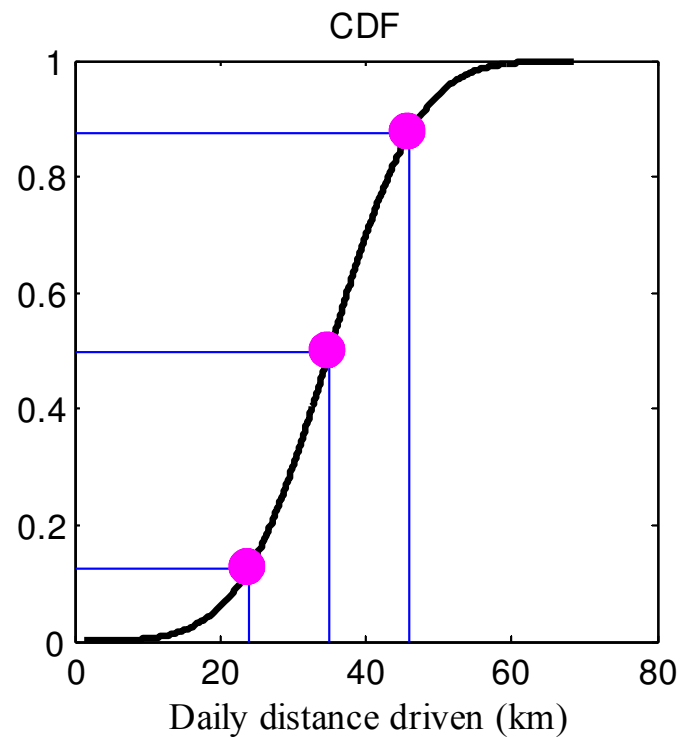
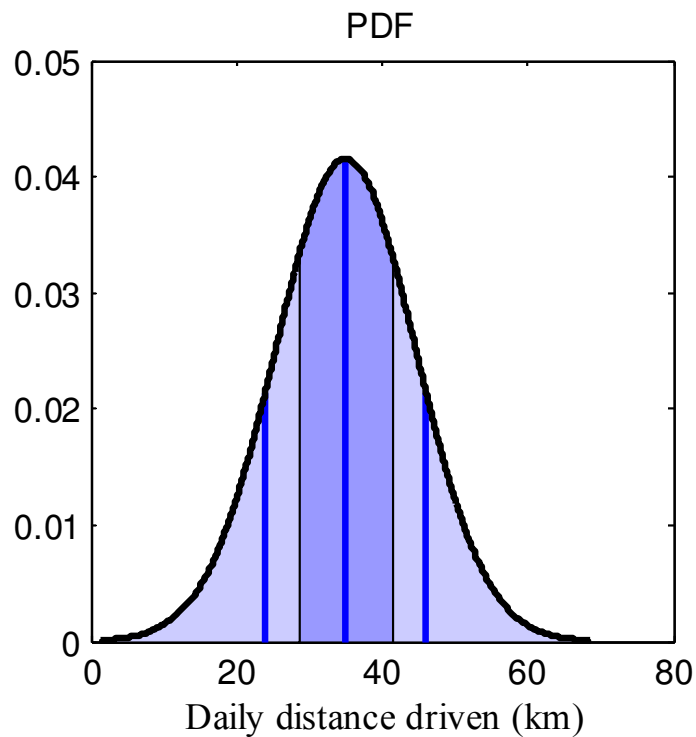
- 3 groups (from mobility studies)

Type	Beginning hour	Ending hour	Duration	Percentage of PEVs
1	16:00	7:00 (next day)	16 hours	45 %
2	21:00	7:00 (next day)	11 hours	40 %
3	2:00	21:00	19 hours	15 %

# Input data

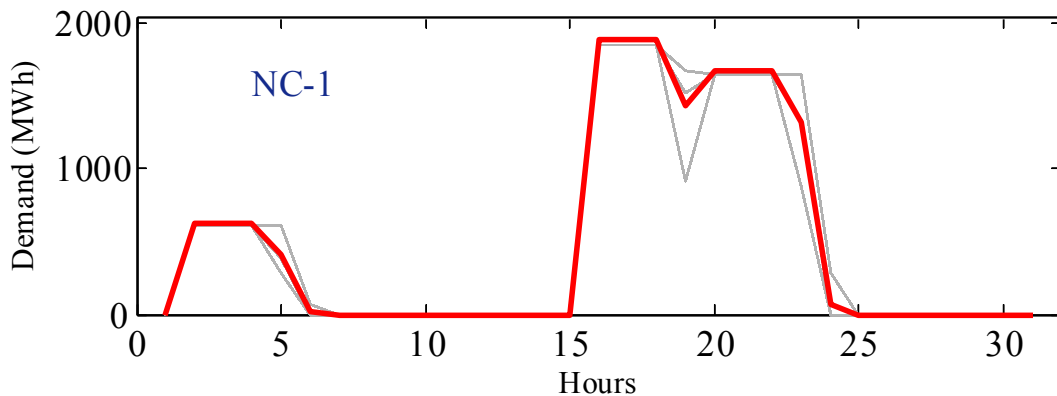
- Daily driven distance:  $N(35, 9.6)$

(G. Tal, M. A. Nicholas, J. Davies, J. Woodjack, 2014)

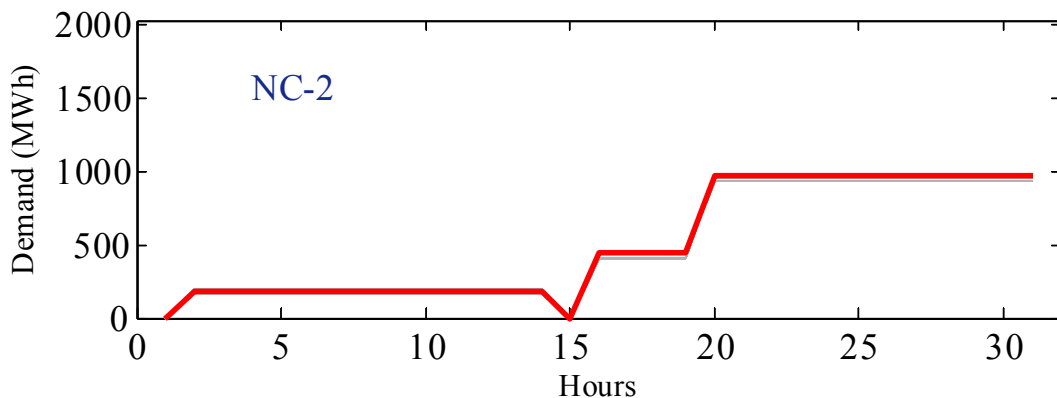


# Input data

## PEVs demand



- **NC-1:** Charging starts when PEVs are available to be charged
  - Demand peaks



- **NC-2:** Charging is evenly distributed during all periods in which PEVs are available to be charged
  - Smooth demand

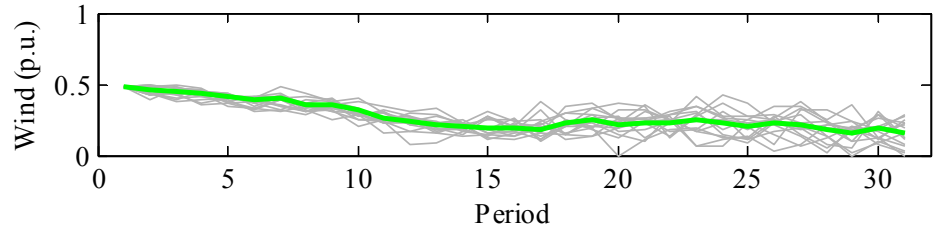
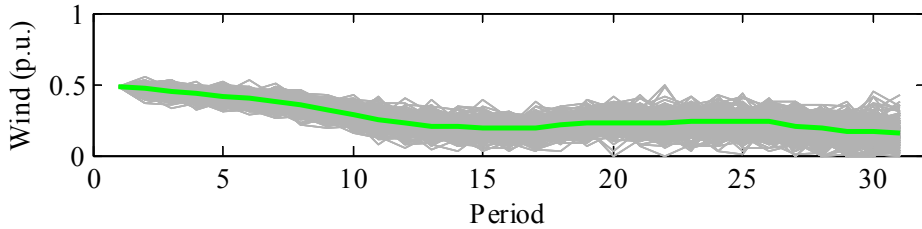
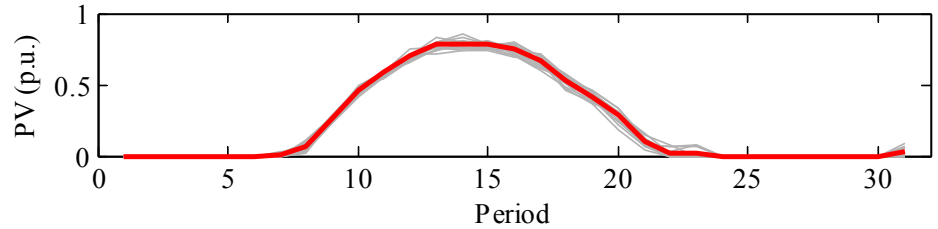
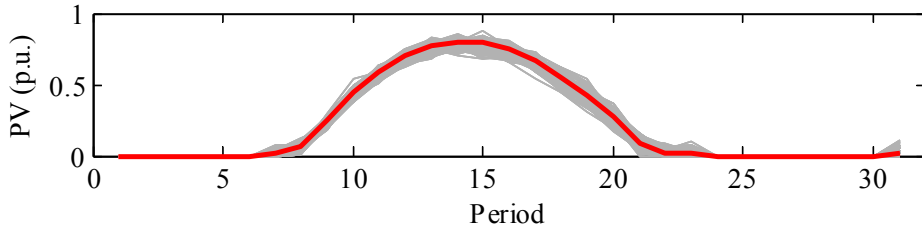
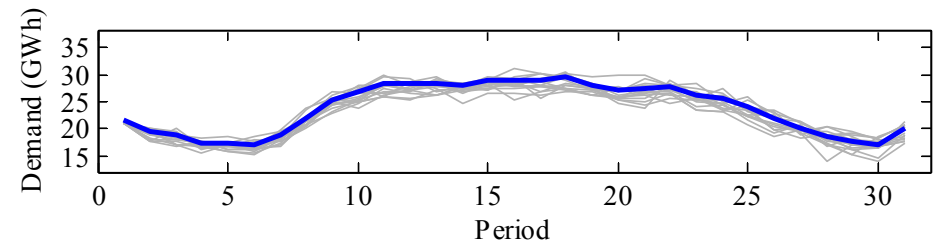
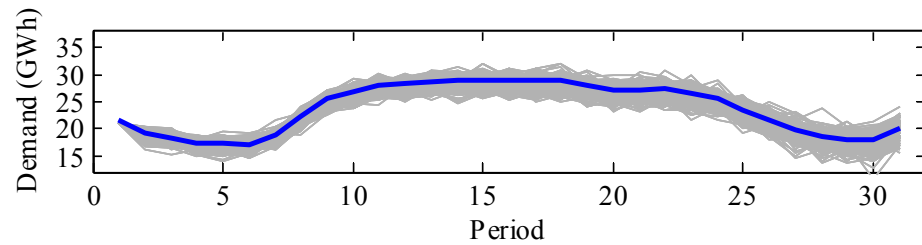
# Input data

## □ Uncertain parameters (Morales et al., 2009)

Initial set (600 scenarios)



Final set (15 scenarios)



# Solution

## □ Computational size

- Constraints: 1.8 millions
- Continuous variables: 1.6 millions

## □ CPLEX 12.2.0.1

- Server with four 2.9 GHz and 250 GB of RAM

## □ Solution time

- Between 1.3 and 4.5 hours

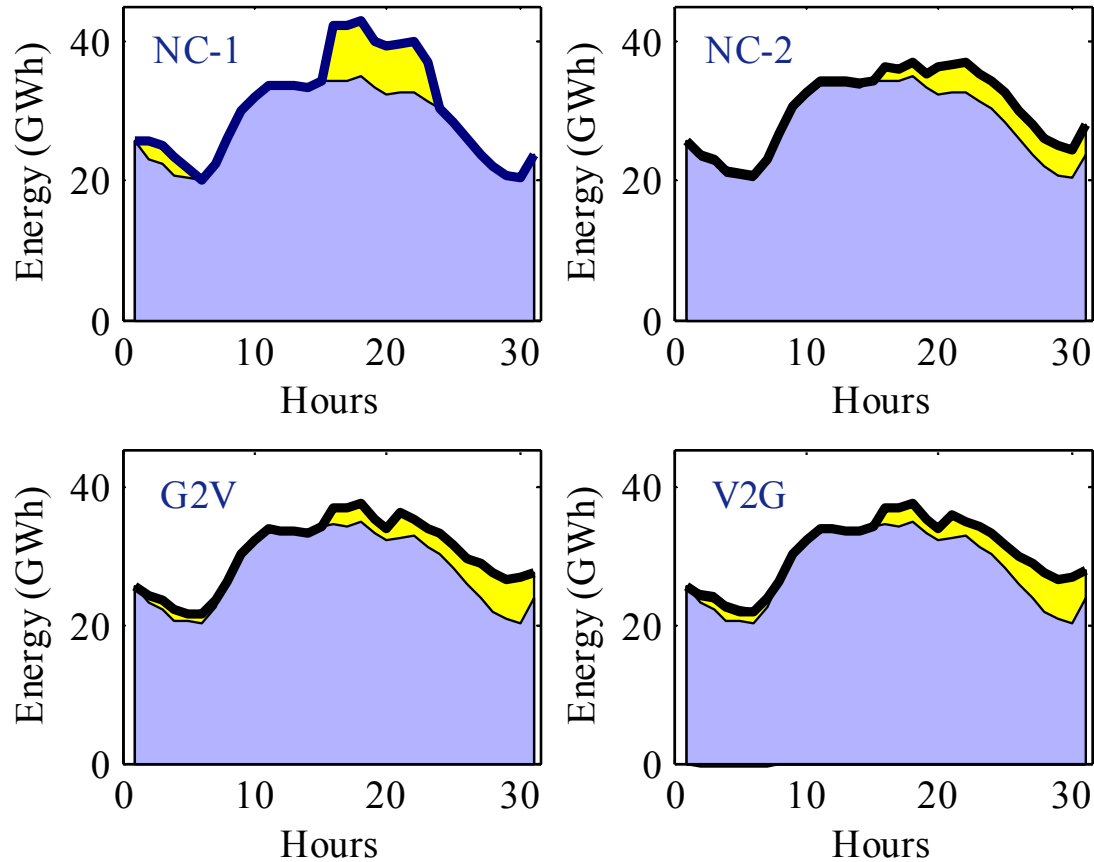


# Expected generation costs

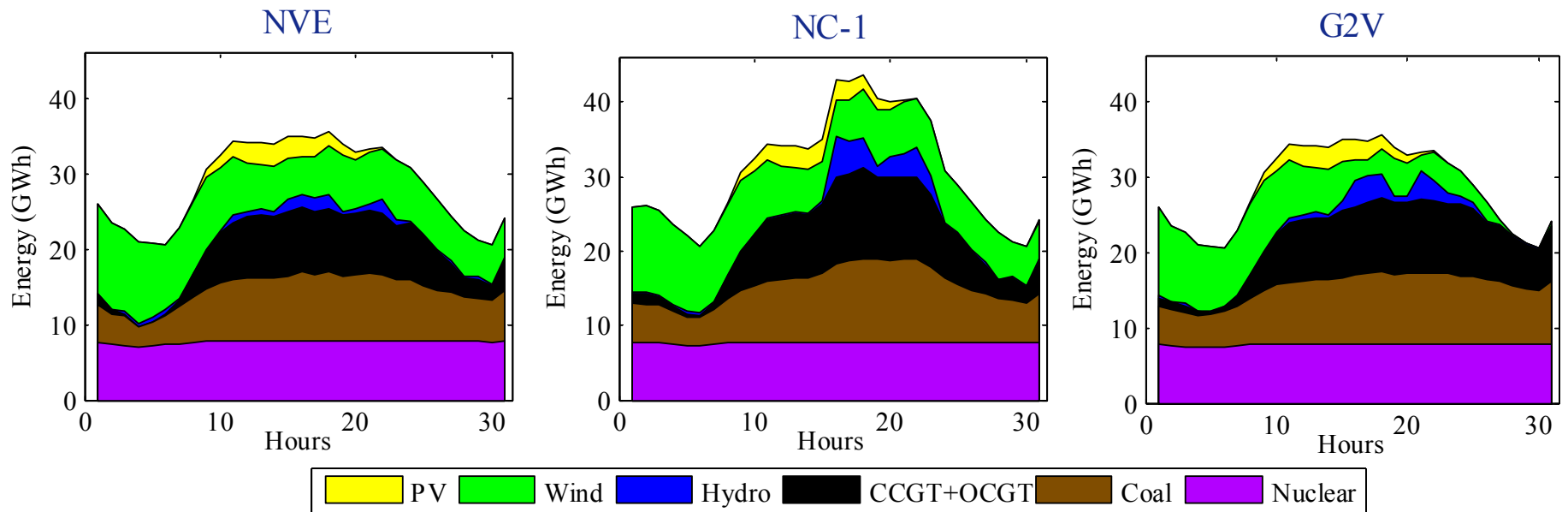
	Non-PEV	NC-1	NC-2	G2V	V2G
Expected cost (M€)	11.480	13.830	13.638	13.359	13.342

- ❑ Increment of 7.6% in the total demand (66.4 GWh)
- ❑ The expected cost increases between 16.2 and 20.5%
- ❑ The coordination G2V reduces the cost between 3.4 and 2.0%
- ❑ V2G does not outperform G2V significantly (0.1%)

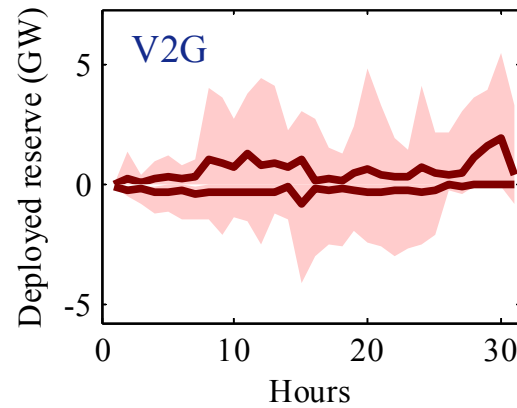
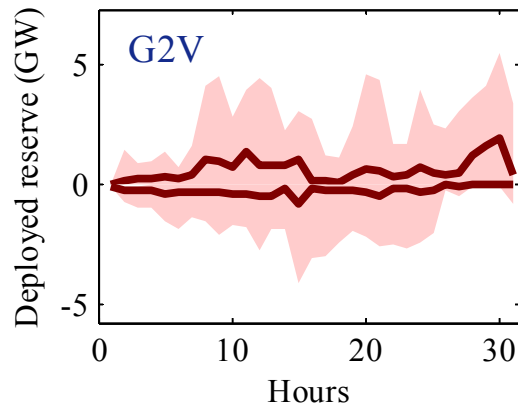
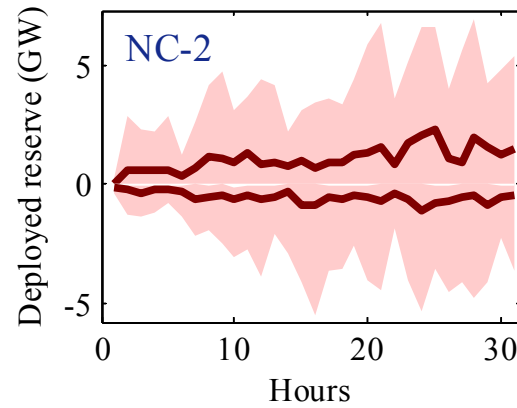
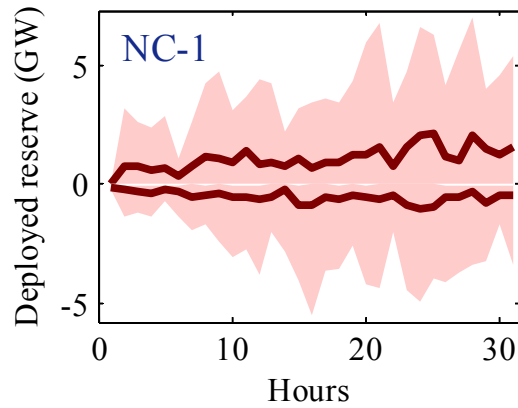
# Expected demand profile



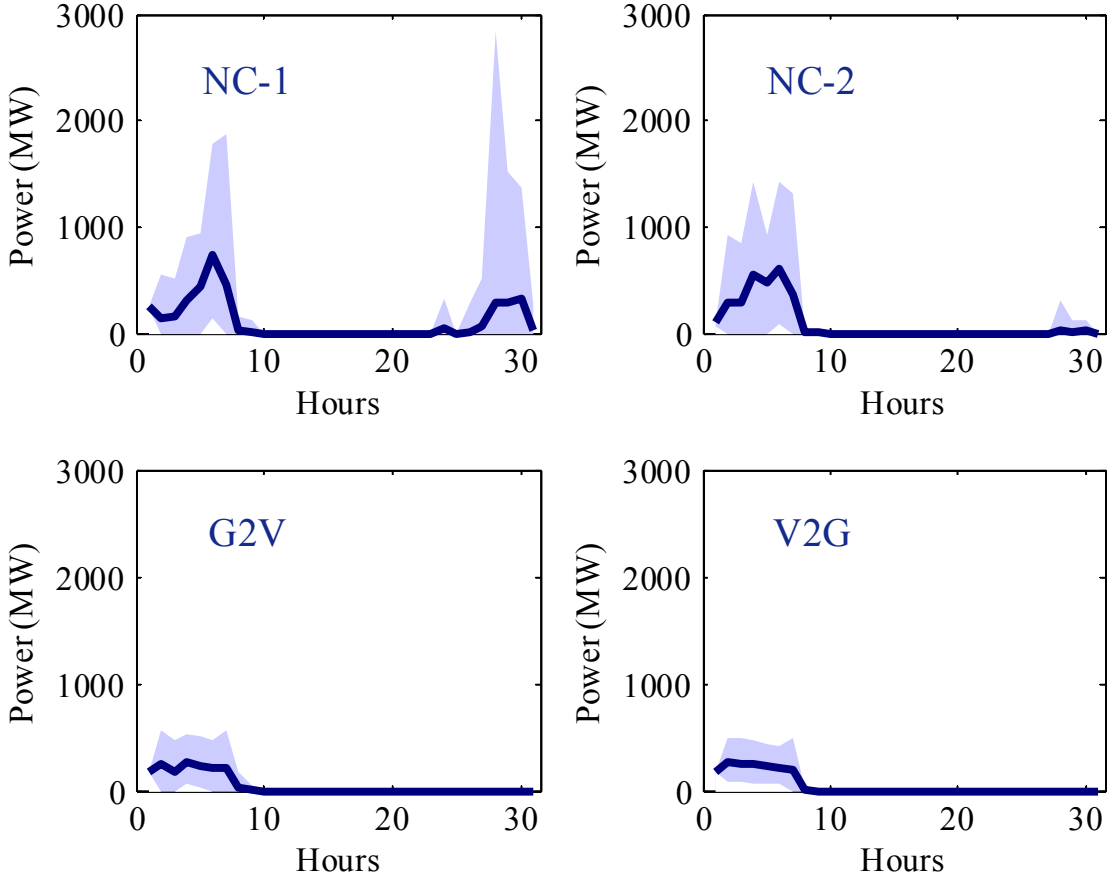
# Day-ahead schedule



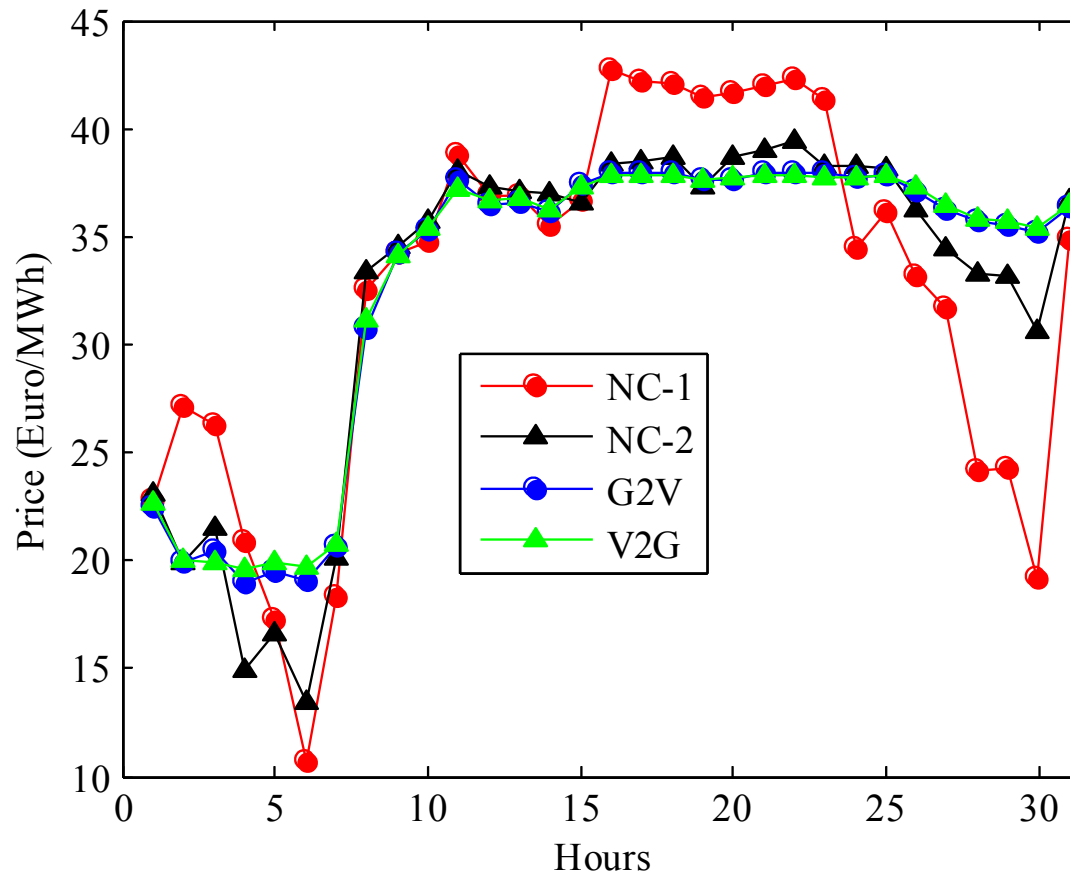
# Reserve deployment



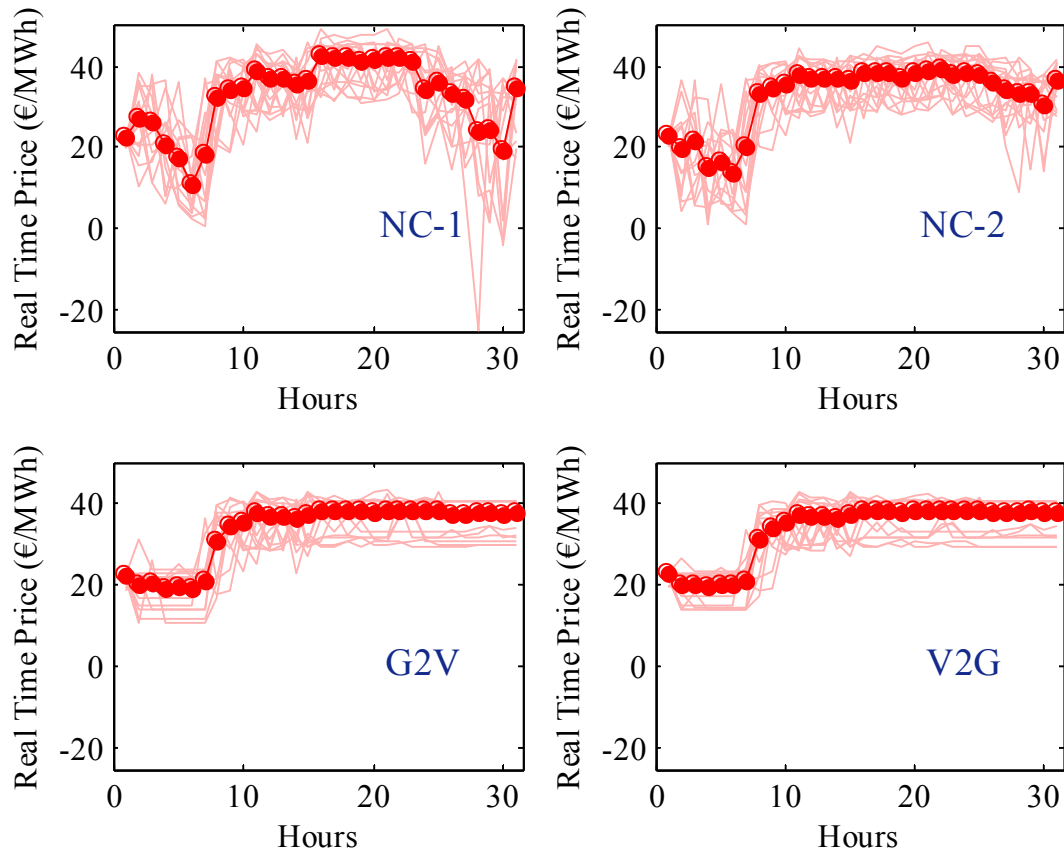
# Wind spillage



# Day-ahead prices



# Real-time prices



# Consumers payments

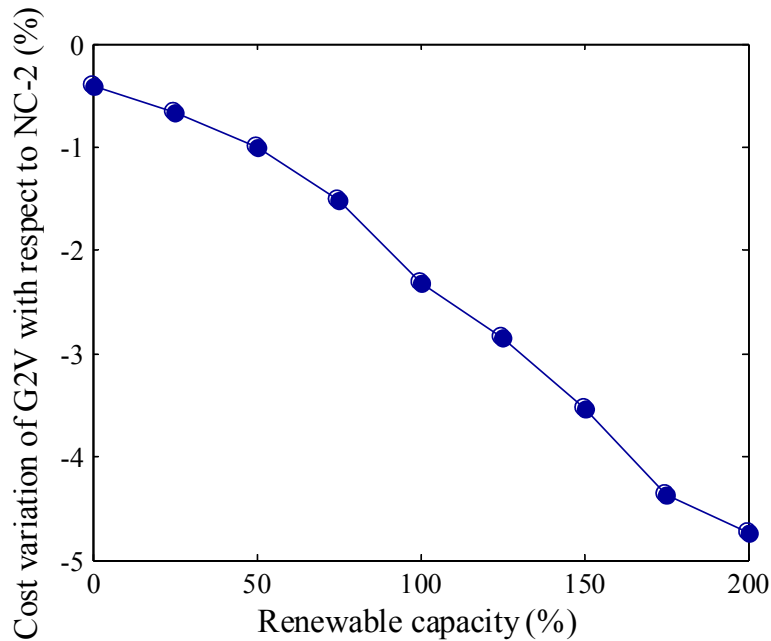
## Expected payment (M€)

	Non-PEV	NC-1	NC-2	G2V	V2G
Total	27.202	31.613	31.150	31.095	31.123
PEVs	0.000	2.539	2.255	2.214	2.221
Non PEVs	27.202	29.074	28.894	28.881	28.902

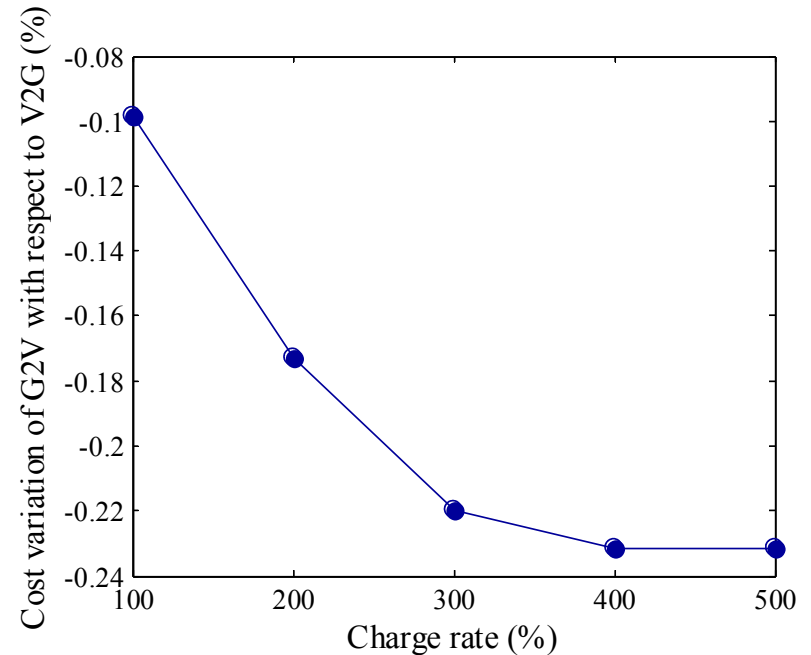


# Sensitivity analysis

Renewable capacity  
(G2V versus NC-2)

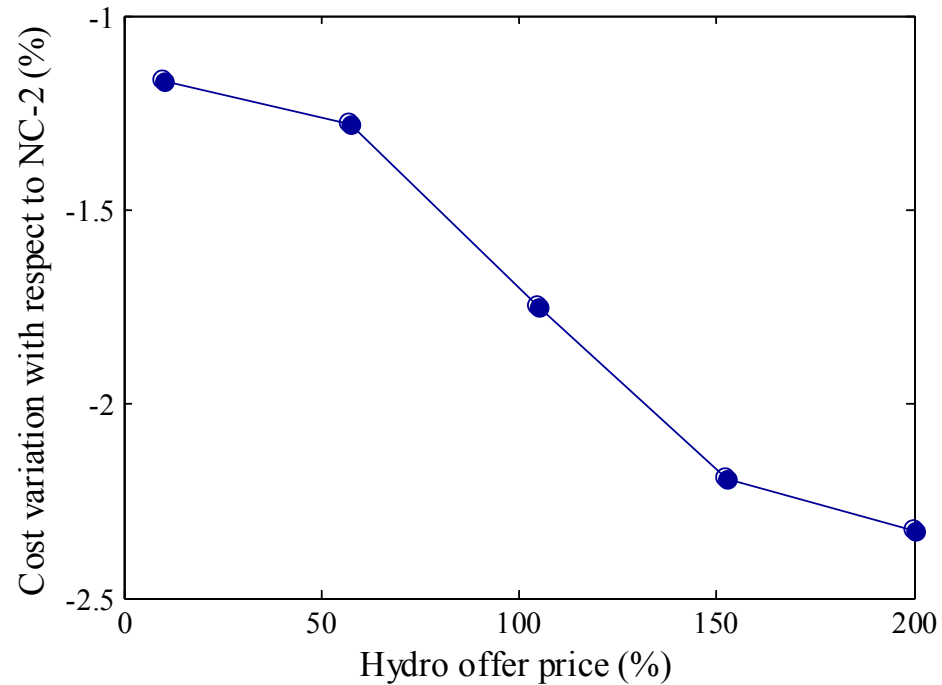


Peak power charge rate  
(G2V versus V2G)

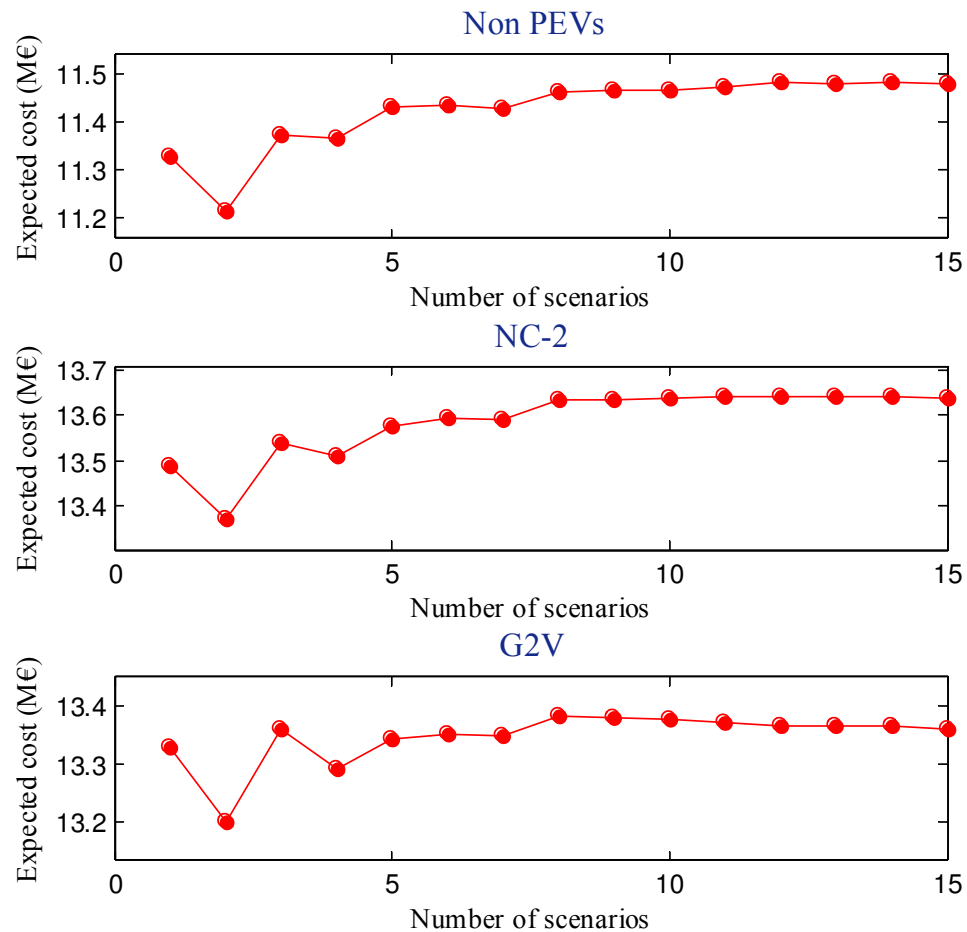


# Sensitivity analysis

Hydro offer cost  
(G2V versus NC-2)



# Number of scenarios



# Conclusions

- ❑ For the studied day, the coordination between the Independent System Operator and the PEVs:
  - Reduces the expected costs
  - Reduces the wind spillage and the usage of deployed reserves
  - Reduces the difference between peak and valley day-ahead prices
  - Reduces the volatility of real-time prices
  - Is appropriated for those power systems with a significant amount of renewable resources
  
- ❑ The coordination V2G does not outperform G2V significantly
  
- ❑ Solution times are high if coordination is taken into account

# Further details

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Operation of renewable-dominated power systems with a significant penetration of plug-in electric vehicles



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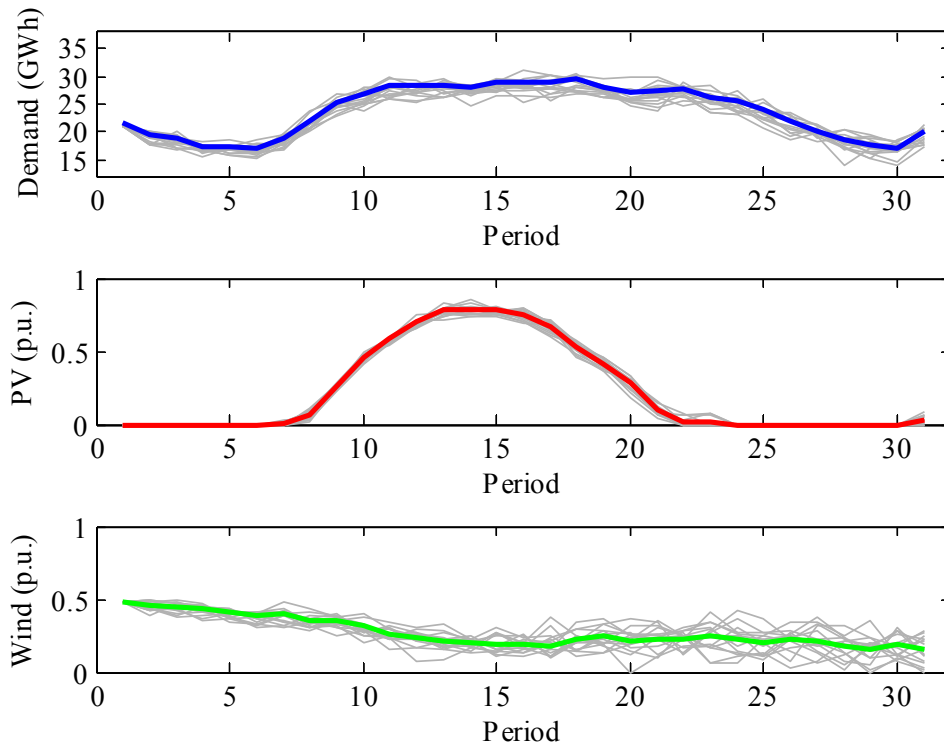
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Thanks very much for your  
attention!

# Input data

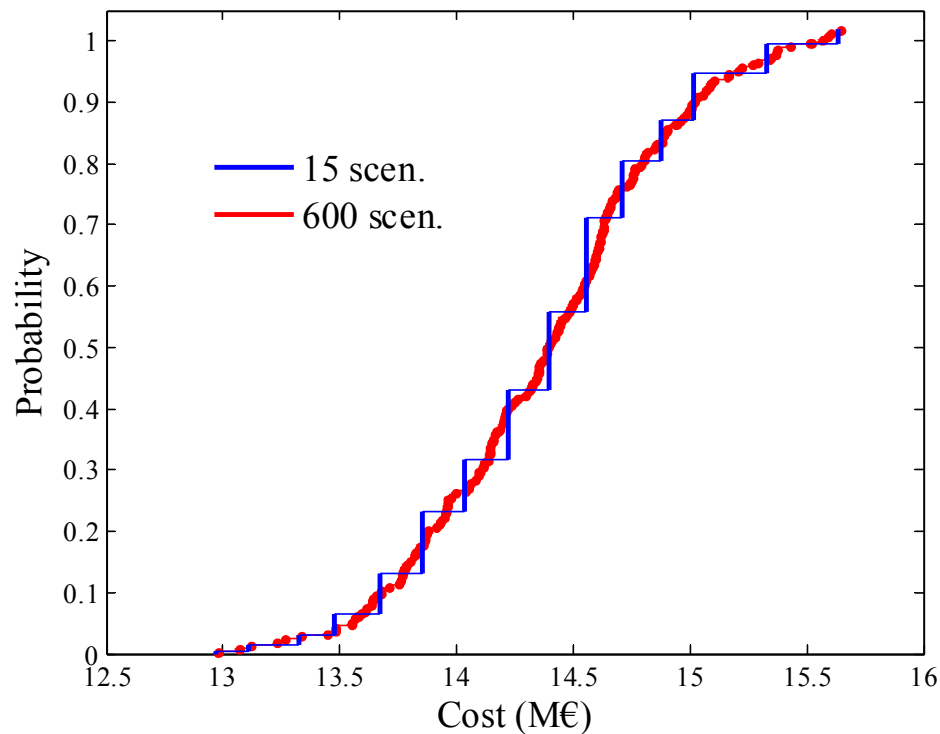
## □ Uncertainty



- Initial set: 600 (3 x 200) scenarios
- Final set: 15 scenarios (Morales et al., 2009)

# Input data

- Initial set of 600 (3 x 200) scenarios
  - Scenario reduction (Morales et al., 2009)





# Example for one scenario

