

Analysis of the Impact of Sub-Hourly Unit Commitment on Power System Dynamics

T. Kërçi^a, J. Giraldo^b, F. Milano^{a,*}

^a*School of Electrical and Electronic Engineering, University College Dublin, Ireland*

^b*Eindhoven University of Technology, Netherlands*

Abstract

This paper discusses the impact of the sub-hourly unit commitment problem on power system dynamics. Such an impact is evaluated by means of a co-simulation platform that embeds a sub-hourly stochastic mixed-integer linear programming security constrained unit commitment (sSCUC) into a time domain simulator, as well as includes a rolling planning horizon that accounts for forecast updates. The paper considers different sub-hourly sSCUC resolutions (i.e., 5 and 15 minutes) and different wind penetration levels (i.e., 25 and 50%). The focus is on the transient response of the system and on frequency variations following different sSCUC strategies, and different sSCUC wind power uncertainty and volatility. The case study consists of a comprehensive set of Monte Carlo simulations based on the 39-bus system.

Keywords: Co-simulation, dynamic performance, frequency stability, sub-hourly unit commitment, stochastic programming.

1. Introduction

Transmission system operators (TSOs) rely on hourly unit commitment (UC) models to economically operate the system [1]. Since large amounts of stochastic renewable energy sources (RES) can significantly impact on the performance of the system [2, 3], stochastic programming has been introduced in

*Corresponding author

Email addresses: taulant.kerci@ucdconnect.ie (T. Kërçi), federico.milano@ucd.ie (F. Milano)

6 recent years to properly account for uncertainty (e.g., wind) when scheduling
7 the system [4]. For example, [5] shows that using a stochastic UC leads to de-
8 crease the operating cost and improve system performance. In [6], the authors
9 show that a stochastic market-clearing procedure allows greater wind penetra-
10 tion compared to a deterministic approach.

11 A recent trend in the economic dispatch of power systems with high pen-
12 etration of RES is the utilization of sub-hourly scheduling as opposed to the
13 conventional hourly dispatch [7, 8]. This is what is currently happening in the
14 European electricity market where more and more energy is being traded closer
15 to real time (e.g., intraday) [9]. According to the European Electricity Balanc-
16 ing guideline [10], all EU countries should implement an Imbalance Settlement
17 Period (ISP) of 15 minutes (i.e., switch from one hour to 15 minutes) by no later
18 than Q4 2020. Likewise, the Australian Energy Market Operator (AEMO) is
19 planning to use a 5 minute ISP by mid of 2021 [11].

20 The sub-hourly scheduling is a way to increase flexibility without investing
21 in physical assets [12, 13]. In [14], it is shown that sub-hourly modeling allows
22 to better capture the costs and the ramping capability of generators. In [15],
23 it is shown that sub-hourly dispatch results in lower costs and lower reserves.
24 The importance of sub-hourly modeling is also shown in [16], where the authors
25 conclude that sub-hourly modeling reveal significant power plant cycling in the
26 form of ramping and start-ups.

27 The works above study the impact of the sub-hourly modeling in power
28 systems from the economic and/or operational point of view. The focus of
29 our work, on the other hand, is on the impact of the sub-hourly UC on power
30 system dynamics. If sub-hourly scheduling timescales are used, say 15-minute
31 or 5-minute, in fact, then these timescales can overlap with long-term dynamics
32 [17]. Therefore, it appears useful and timely to embed the UC problem into
33 a fully-fledged transient stability analysis software tool [18, 19], and study the
34 dynamic behaviour of power systems.

35 In the literature, this goal has been studied by including linear constraints
36 into the UC formulation [20]. For example, [21] shows that, by including a

37 frequency ramp limit constraint (RoCoF) in the UC formulation, frequency is
38 kept within its limits. Similarly, [22] shows that the inclusion of frequency
39 constraints in the UC problem significantly affects UC decisions and lead to
40 higher operating costs. The works above fail to capture the long-term frequency
41 deviations of the system that are an important concern for system operators
42 [23, 24].

43 Modern power systems embed different technologies such as communication
44 networks, demand-side management, electric vehicles, and RES. Co-simulation
45 is seen as a useful method to study the interactions of such complex systems
46 [25]. This is due to the fact that a co-simulation approach allows the coupling of
47 different subdomain models (e.g., power systems and electricity markets), where
48 each subdomain is described and solved within its native environment without
49 the need of simplifying one or another [26, 27]. For example, in [28] the authors
50 propose a simulation platform that couples continuous power system simula-
51 tors with discrete communication network simulators. In [29], a co-simulation
52 method that couples electromagnetic transient and dynamic phasor simulations
53 is proposed.

54 *1.1. Contributions*

55 The main contributions of this paper are the following:

- 56 • The development of a flexible co-simulation platform that allows evaluat-
57 ing the impact that different stochastic scenarios to model wind generation
58 as well as different sub-hourly resolutions included in a UC problem have
59 on power system dynamics.
- 60 • A comprehensive sensitivity analysis of the interaction between sub-hourly
61 UC and power system dynamics based on Monte Carlo time domain sim-
62 ulations of stochastic differential-algebraic equations.

63 The proposed co-simulation platform is a tool aimed at helping TSOs to decide
64 which UC problem (e.g., deterministic vs stochastic) is more adequate for their
65 grid depending on the renewable penetration and the planning horizon. With

66 this aim, the paper compares various UC problem implementations with differ-
 67 ent approaches to handle uncertainty and volatility and discuss their impact on
 68 the long-term frequency deviations of the system.

69 1.2. Organization

70 The remainder of the paper is organized as follows. Section 2 describes
 71 the dynamic model of power systems based on stochastic differential algebraic
 72 equations (SDAEs); the modelling of stochastic processes; the mathematical for-
 73 mulation of the mixed-integer linear programming (MILP) stochastic security-
 74 constrained unit commitment (sSCUC); and the modelling of the sSCUC un-
 75 certainty and volatility, and rolling planning horizon. Section 2 also shows how
 76 the sSCUC and SDAEs interact together. The results of the case studies based
 77 on the IEEE 39-bus system are discussed in Section 3. Conclusions and future
 78 work are given in Section 4.

79 2. Modeling

80 2.1. Power system model

81 Power system dynamics with inclusion of stochastic processes can be modeled
 82 as a set of hybrid stochastic differential-algebraic equations (SDAEs) [30]:

$$\begin{aligned}
 \dot{\mathbf{x}} &= \mathbf{f}(\mathbf{x}, \mathbf{y}, \mathbf{u}, \mathbf{z}, \dot{\boldsymbol{\eta}}) \\
 \mathbf{0} &= \mathbf{g}(\mathbf{x}, \mathbf{y}, \mathbf{u}, \mathbf{z}, \boldsymbol{\eta}) \\
 \dot{\boldsymbol{\eta}} &= \mathbf{a}(\mathbf{x}, \mathbf{y}, \boldsymbol{\eta}) + \mathbf{b}(\mathbf{x}, \mathbf{y}, \boldsymbol{\eta}) \boldsymbol{\xi},
 \end{aligned} \tag{1}$$

83 where \mathbf{f} are the differential equations; \mathbf{g} are the algebraic equations; \mathbf{x} are the
 84 state variables, e.g. generator rotor speeds; \mathbf{y} are the algebraic variables, e.g. bus
 85 voltage angles; \mathbf{u} are the inputs, e.g. load forecast and active power schedules;
 86 \mathbf{z} are discrete variables, e.g. status of the machines); $\boldsymbol{\eta}$ represent stochastic
 87 perturbations, e.g. wind speed variations, which are modeled through the last
 88 term in (1); \mathbf{a} and \mathbf{b} represent the *drift* and *diffusion* of the stochastic differential
 89 equations (SDEs), respectively; and $\boldsymbol{\xi}$ represent the white noise vector.

90 Equations (1) are solved using numerical integration techniques for SDAEs.
 91 Since our analysis is based on long-term dynamic simulations, it is desirable
 92 that the model includes both electro-mechanical models and long-term dynam-
 93 ics models. In particular, (1) includes the dynamic models of synchronous ma-
 94 chines, turbine governors (TGs), automatic voltage regulators, power system
 95 stabilizers, wind power plants, automatic generation control (AGC), and the
 96 discrete model of sSCUC. These are standard models used for transient sta-
 97 bility analysis that are found, for example, in EuroStag and PSS/E software.
 98 TGs are modelled as a conventional droop (R) and a lead-lag transfer function,
 99 whereas the AGC is represented by an integrator with gain k_o . Wind power
 100 plants are represented by aggregated models, which implement a 5-th order
 101 Doubly-Fed Induction Generator (DFIG) with voltage, pitch angle and MPPT
 102 controllers [31].

103 2.2. Modelling of stochastic processes

104 Modelling the stochastic nature of wind power is critical in power system
 105 dynamic studies [32]. In this context, (1) includes only wind power variations
 106 with respect to the forecast wind generation as a stochastic perturbations. An
 107 Ornstein-Uhlenbeck Process (OUP) is used to model the stochastic nature of
 108 the wind speed v_s that enters into the wind turbine, as follows:

$$\begin{aligned}
 v_s(t) &= v_{s0} + \eta_v(t) \\
 \dot{\eta}_v(t) &= \alpha_v(\mu_v - \eta_v(t)) + b_v \xi_v
 \end{aligned}
 \tag{2}$$

109 where v_{s0} is the wind speed initial value; η_v is the stochastic variable that is
 110 dependent on the drift $\alpha_v(\mu_v - \eta_v)$, and diffusion term b_v of the SDEs; α is
 111 the mean reversion speed that indicates the rate at which η_v tends to the mean
 112 value μ_v ; and ξ_v represents the white noise.

113 2.3. Stochastic Unit Commitment Formulation

114 As the penetration of highly variable RES increases so does the uncertainty
 115 in power systems. This complicate the real-time balance between generation

116 and demand. Therefore it is of particular importance to model the uncertainty
 117 when scheduling the system. There are different methodologies and techniques
 118 proposed for optimization under uncertainty, with one of the most popular be-
 119 ing the two-stage stochastic programming. In the context of UC, the two-stage
 120 stochastic UC makes use of a probabilistic model for the uncertain input param-
 121 eters, e.g. wind generation, and is usually approximated by a set of scenarios
 122 representing the plausible realizations of these random parameters [4].

In this work, a standard MILP sSCUC problem is implemented based on [33], in which wind power production is considered as an uncertain parameter of the system, as follows:

$$\begin{aligned} & \min_{H,W} \sum_{t \in \mathcal{T}} \sum_{g \in \mathcal{G}} (C_g^F z_{g,t}^F + C_g^{SU} z_{g,t}^{SU} + C_g^{SD} z_{g,t}^{SD}) \quad (3) \\ & + \sum_{\omega \in \Omega} \pi_{\omega} \left[\sum_{t \in \mathcal{T}} \sum_{l \in \mathcal{L}} C_g^V p_{g,t,\omega} + \sum_{t \in \mathcal{T}} \sum_{l \in \mathcal{L}} C^L L_{l,t,\omega}^{SH} \right] \end{aligned}$$

such that

$$z_{g,t}^{SU} - z_{g,t}^{SD} = z_{g,t}^F - z_{g,t-1}^F \quad (4)$$

$$(\forall g \in \mathcal{G}, \forall t \in \{2, \dots, T\})$$

$$z_{g,t}^{SU} - z_{g,t}^{SD} = z_{g,t}^F - IS_g \quad (5)$$

$$(\forall g, \forall t \in \{1\})$$

$$z_{g,t}^{SU} + z_{g,t}^{SD} \leq 1 \quad (6)$$

$$(\forall g, \forall t \in \{1, \dots, T\})$$

$$z_{g,t}^F = IS_g \quad (7)$$

$$(L_g^{UP} + L_g^{DW} > 0, \forall g, \forall t \leq L_g^{UP} + L_g^{DW})$$

$$\sum_{\tau=t-UT_g+1}^t z_{g,\tau}^{SU} \leq z_{g,t}^F \quad (8)$$

$$(\forall g, \forall t > L_g^{UP} + L_g^{DW})$$

$$\sum_{\tau=t-DT_g+1}^t z_{g,\tau}^{SD} \leq 1 - z_{g,t}^F \quad (9)$$

$$(\forall g, \forall t > L_g^{UP} + L_g^{DW})$$

$$\begin{aligned} \sum_{g \in \mathcal{G}_n} p_{g,t,\omega} - \sum_{l \in \mathcal{L}_n} L_{l,t} + \sum_{l \in \mathcal{L}_n} L_{l,t,\omega}^{SH} + \sum_{f \in \mathcal{F}_n} W_{f,t,\omega} \\ - \sum_{f \in \mathcal{F}_n} W_{f,t,\omega}^{SP} = \sum_{m \in \mathcal{M}_n} \frac{(\delta_{n,t,\omega} - \delta_{m,t,\omega})}{X_{n,m}} \end{aligned} \quad (10)$$

$$(\forall n, \forall t, \forall \omega \in \Omega)$$

$$p_{g,t,\omega} \leq P_g^{\max} z_{g,t}^F \quad (11)$$

$$(\forall g, \forall t, \forall \omega \in \Omega)$$

$$p_{g,t,\omega} \geq P_g^{\min} z_{g,t}^F \quad (12)$$

$$(\forall g, \forall t, \forall \omega \in \Omega)$$

$$p_{g,t,\omega} \leq (P_g^{IS} + RU_g) z_{g,t}^F \quad (13)$$

$$(\forall g, \forall t \in \{1\}, \forall \omega \in \Omega)$$

$$p_{g,t,\omega} \geq (P_g^{IS} - RD_g) z_{g,t}^F \quad (14)$$

$$(\forall g, \forall t \in \{1\}, \forall \omega \in \Omega)$$

$$p_{g,t,\omega} - p_{g,t-1,\omega} \leq (2 - z_{g,t-1}^F - z_{g,t}^F) P_g^{SU} \quad (15)$$

$$+ (1 + z_{g,t-1}^F - z_{g,t}^F) RU_g$$

$$(\forall g, \forall t \in \{2, \dots, T\}, \forall \omega \in \Omega)$$

$$p_{g,t-1,\omega} - p_{g,t,\omega} \leq (2 - z_{g,t-1}^F - z_{g,t}^F) P_g^{SD} \quad (16)$$

$$+ (1 - z_{g,t-1}^F + z_{g,t}^F) RD_g$$

$$(\forall g, \forall t \in \{2, \dots, T\}, \forall \omega \in \Omega)$$

$$L_{l,t,\omega}^{SH} \leq L_{l,t} \quad (17)$$

$$(\forall l, \forall t, \forall \omega \in \Omega)$$

$$W_{f,t,\omega}^{SP} \leq W_{f,t,\omega} \quad (18)$$

$$(\forall f, \forall t, \forall \omega \in \Omega)$$

$$-P_{n,m}^{\max} \leq \frac{(\delta_{n,t,\omega} - \delta_{m,t,\omega})}{X_{n,m}} \leq P_{n,m}^{\max} \quad (19)$$

$$(\forall n, m \in M_n, \forall t, \forall \omega \in \Omega)$$

$$p_{g,t,\omega}, L_{i,t,\omega}^{SH}, W_{f,t,\omega}^{SP} \geq 0 \quad (20)$$

$$(\forall g, \forall l, \forall f, \forall t, \forall \omega \in \Omega)$$

$$z_{g,t}^F, z_{g,t}^{SU}, z_{g,t}^{SD} \in \{0, 1\} \quad (21)$$

$$(\forall g, \forall t)$$

and the initial state conditions are as follows:

$$IS_g = \begin{cases} 1 & \text{if } ON_g > 0 \\ 0 & \text{if } ON_g = 0 \end{cases}$$

$$L_g^{UP} = \min\{T, (UT_g - ON_g)IS_g\}$$

$$L_g^{DW} = \min\{T, (DT_g - OFF_g)(1 - IS_g)\}$$

123 Equations (3) represent the total cost to be minimized which includes the fixed,
 124 start-up, shut-down and variable cost of the generating units, as well as the cost
 125 of involuntarily demand curtailment. Equations (4)-(6) model the logical ex-
 126 pression between the binary variables (i.e., start-up and shut-down of generating
 127 units). Equations (7)-(9) model the minimum and maximum up- and down-time
 128 constraints. The power balance constraint is modeled through equations (10).
 129 While the capacity limits of generating units are modeled through equations
 130 (11)-(12) and their respective ramping limits through (13)-(16). Equations (17)-
 131 (18) model the limits of the involuntary demand curtailment and wind power
 132 spillage, respectively. Transmission capacity limits are enforced by equations
 133 (19). Finally, equations (20)-(21) refer to the variable declarations.

134 The model shown in (3)-(21) is the deterministic equivalent of the original
 135 two-stage stochastic programming problem. It is called a two-stage problem
 136 since there are first-stage and second-stage variables, also known as here-and-
 137 now and wait-and-see variables, respectively [4]. In particular, $z_{g,t}^F, z_{g,t}^{SU}, z_{g,t}^{SD}$
 138 are first-stage decision variables that represent the status of generating unit g

139 in time period t (i.e., ON/OFF status, start-up and shut-down). These deci-
 140 sions do not depend on uncertainty realization ω , and are generally made one
 141 day in advance. Similarly, $p_{g,t,\omega}$, $L_{l,t,\omega}^{SH}$, $W_{f,t,\omega}^{SP}$, $\delta_{n,t,\omega}$ are second-stage decision
 142 variables that represent the active power dispatch of generating units g in time
 143 period t and scenario ω , the involuntary power curtailment from load l in time
 144 period t and scenario ω , wind power spillage from wind production unit f in
 145 time period t and scenario ω , and voltage angle at node n in time period t and
 146 scenario ω , respectively. All second-stage decision variables depend on uncer-
 147 tainty realization ω . Further details of the sSCUC can be found in [33] and
 148 references therein.

149 2.4. Scenarios and Rolling Horizon within the sSCUC

To illustrate the modelling of sSCUC wind uncertainty and volatility, and
 rolling planning horizon used in this paper, we show below the power balance
 equations of the sSCUC, as follows:

$$\begin{aligned} & \sum_{g \in \Omega_{G_n}} p_{g,t,\omega} - \sum_{l \in \Omega_{L_n}} L_{l,t} + \sum_{l \in \Omega_{L_n}} L_{l,t,\omega}^{SH} + \sum_{k \in \Omega_{K_n}} W_{k,t,\omega} \\ & - \sum_{k \in \Omega_{K_n}} W_{k,t,\omega}^{SP} = \sum_{m \in \Omega_{M_n}} \frac{(\delta_{n,t,\omega} - \delta_{m,t,\omega})}{X_{n,m}}, (\forall n, \forall t, \forall \omega \in \Omega) \end{aligned} \quad (22)$$

150 where $p_{g,t,\omega}$ is the active power of conventional generating units g , at time
 151 period t , and scenario ω (i.e., equivalent of the second-stage variable $u_{f,t,\omega}$ in
 152 section 2.3); $L_{l,t}$ is the demand for load l at time period t ; $L_{l,t,\omega}^{SH}$ is the power
 153 curtailment from load l , at time period t , and in scenario ω ; $W_{k,t,\omega}$ and $W_{k,t,\omega}^{SP}$
 154 represent the power generation and curtailment, respectively, from wind unit
 155 k , in time period t , and scenario ω ; $X_{n,m}$ is the reactance of line $n - m$; $\delta_{n,t,\omega}$
 156 represent the voltage angle at node n , time period t , and scenario ω ; and Ω_{K_n} ,
 157 Ω_{M_n} are the sets of stochastic power generation (i.e., wind) located at node n ,
 158 and nodes $m \in N$ connected to node n by transmission line, respectively.

159 2.4.1. Modelling wind uncertainty

160 Similar to [34], a wind power penetration level $W_{k,t,\omega}$ is defined as a per-
 161 centage of the demand $L_{l,t}$, and named the medium scenario, $W_{k,t,\omega}^M$. Then,

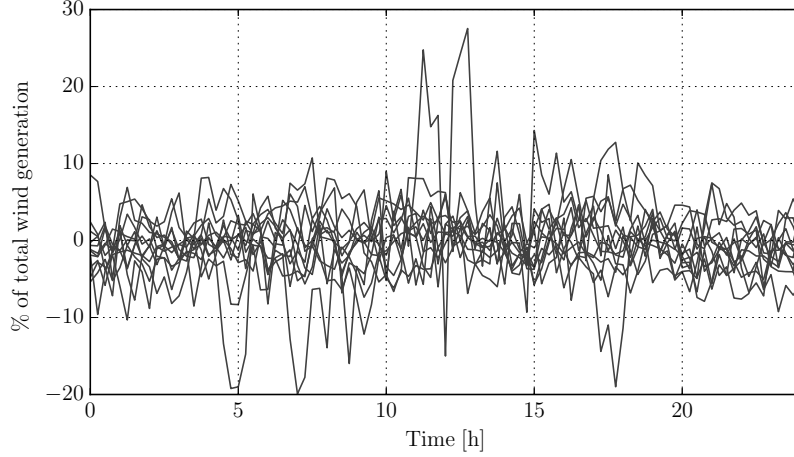


Figure 1: Wind power 15min rate of change for 12 typical day in the Irish system in 2018.

162 high and low wind power scenarios ($W_{k,t,\omega}^H, W_{k,t,\omega}^L$) are built as percentages of
 163 the medium scenario, as follows:

$$\begin{aligned} W_{k,t,\omega}^L &= W_{k,t,\omega}^M \times (1 - j/100) \\ W_{k,t,\omega}^H &= W_{k,t,\omega}^M \times (1 + j/100) \end{aligned} \quad (23)$$

164 where j is the percentage of deviation of the the high and low scenarios with
 165 respect to the medium one.

166 The consistency of the wind power scenarios with real-world information is
 167 compared using wind power data of the Irish system[35]. Specifically, the 15
 168 minute rate of change of wind power is determined based on one typical day
 169 per each month of 2018 (see Fig. 1). Based on these data, wind power does not
 170 appear to be able to change more than 10% in 15 minutes. For this reason, in
 171 the case study, $j = 10\%$ is assumed.

172 2.4.2. Modelling wind volatility

173 Wind power volatility is modelled as small fluctuations with respect to the
 174 average value for a given period. Hence, uncertainty is related to wind power
 175 forecast, e.g. wind scenarios, while volatility is considered as a percentage,

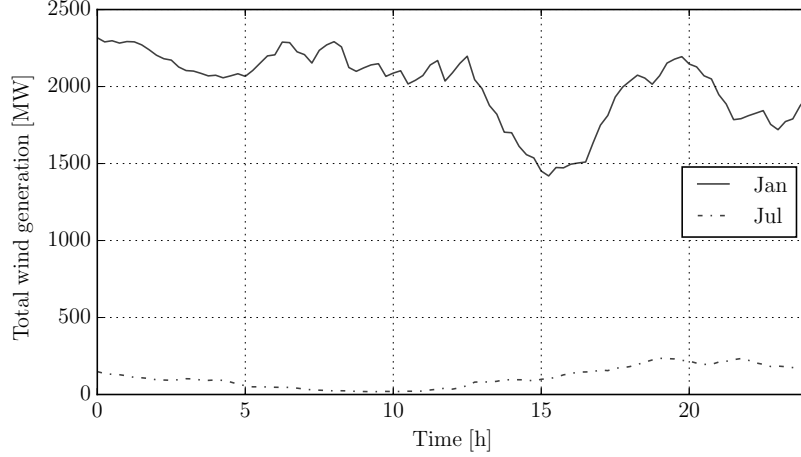


Figure 2: Wind power profile for two typical days (Jan, Jul) in the Irish system in 2018.

176 e.g. standard deviation, on top of the wind power forecast [36]. A normal
 177 distribution $N(\mu, \sigma^2)$ with zero mean and given standard deviation is attached
 178 to each wind power scenario, as follows:

$$\begin{aligned}
 W_{k,t,\omega}^{L1} &= W_{k,t,\omega}^L + N(0, \sigma^2) \\
 W_{k,t,\omega}^{M1} &= W_{k,t,\omega}^M + N(0, \sigma^2) \\
 W_{k,t,\omega}^{H1} &= W_{k,t,\omega}^H + N(0, \sigma^2)
 \end{aligned}
 \tag{24}$$

179 where $W_{k,t,\omega}^{L1}$, $W_{k,t,\omega}^{M1}$, $W_{k,t,\omega}^{H1}$ are the new low, medium and high wind power
 180 scenarios, respectively, after adding the volatility.

181 An important aspect to keep in mind when building the scenarios is the
 182 relationship between the wind power level and its standard deviation σ . With
 183 this aim, two typical days are analysed for two months, namely January (high
 184 wind) and July (low wind). The wind power profile for these typical days is
 185 shown in Fig. 2. It appears that wind varies more in January than in July.
 186 More specifically, the standard deviation of wind power generation is found to
 187 be 234.78 MW and 68.46 MW, for January and July, respectively, and that high
 188 wind leads to higher σ .

189 Note that the goal is not to propose new sSCUC models to deal with wind

190 power uncertainty and volatility, but rather to study the impact of a well as-
 191 sessed sSCUC formulation on power system dynamics. For this reason, it is not
 192 necessary to consider more sophisticated sSCUC models. As a matter of fact,
 193 the case study shows that, depending on the wind penetration and planning
 194 horizon, a sSCUC might not be needed at all.

195 *2.4.3. Modelling the rolling planning horizon*

196 Scheduling the system frequently (i.e., more than once a day) allows having
 197 better wind and load forecasts. As a result, less reserves are required [5]. In this
 198 work, we use a rolling planning approach for updating the wind power forecast
 199 ($W_{k,t,\omega}$) with a planning horizon of 24h. During the first hour of the planning
 200 horizon, the high/low wind scenarios increase/decrease as a linear function from
 201 the medium scenario and after that they have a fixed error, e.g. $j = 10\%$. The
 202 sSCUC model is solved at every time period t during the first 12h with a planning
 203 horizon of 24h. When rolling forward, the status of the units of the previous
 204 horizon serve as an initial status for the next horizon. Between two scheduling
 205 events of the sSCUC, e.g. 15 or 5 minutes, wind and load profiles are modelled
 206 as linear ramps.

207 *2.5. Interaction between sSCUC and SDAEs*

208 It is time to merge all of the above in a single framework. Generally speak-
 209 ing, the goal is to embed equations (3)-(21) and (23)-(24) into equations (1).
 210 One has two ways to do so: embed sSCUC and equations (23)-(24) into an ex-
 211 isting dynamic model, or the other way round. This paper proposes the former
 212 approach, i.e., embedding the sSCUC problem (3)-(21) and equations (23)-(24)
 213 into the TDS routine of DOME [37].

214 The sSCUC model (3)-(21) uses the active power of the generators, namely,
 215 $p_{g,t,\omega}$, as a second-stage decision variable. In other words, $p_{g,t,\omega}$ adapts to the
 216 uncertainty realization ω . Since we are interested in having a single power
 217 dispatch for each generator and for each time period, a reasonable tradeoff
 218 consists in taking a weighted-sum of the scenarios ω . In the literature, one

219 may find different formulations of sSCUC with respect to the active power of
 220 generators. For example, in [38], the authors use the active power as a first-stage
 221 decision variable ($p_{g,t}$, set-points) and then use up/down reserve deployment
 222 (production changes) as a second-stage decision variable to accommodate wind
 223 variability (real-time).

224 Figure 3 shows the overall structure of the recently proposed co-simulation
 225 framework. The tool is composed of two parts, namely, the dynamic model of
 226 power systems (SDAEs) and the discrete model of sSCUC. DOME coordinates
 227 the co-simulation, i.e., the exchange of information between the sSCUC and
 228 the SDAEs. In particular, the output of the sSCUC model, namely, the active
 229 power of generating units, $p_{g,t,\omega}$, serves as an input to the SDAEs, i.e. change
 230 the power set point of the turbine governors of the power plants. Finally, a
 231 Monte Carlo method is utilized to simulate large sets of realizations of the
 232 stochastic processes of wind and loads. Each realization defines the “reality”
 233 that needs to be updated to solve the next sSCUC problem. Such a feedback
 234 is needed to update the forecast of wind ($W_{k,t,\omega}$) and loads as utilized in the
 sSCUC problem.

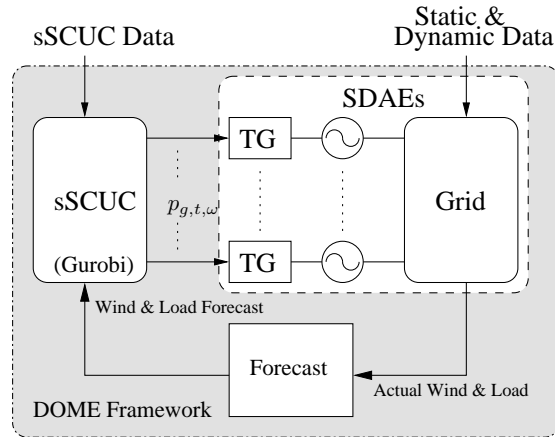


Figure 3: Interaction between the sSCUC problem and the dynamic model of the turbine governors, the synchronous machines and the grid.

236 3. Case studies

237 From a system operator point of view, it is useful to study the impact that
238 different levels of uncertainty and volatility, e.g. wind forecast errors, within
239 the sSCUC model have on power system dynamic performance. Since TSOs
240 still mostly rely on deterministic security-constrained UC (SCUC) formulations,
241 a comparison between SCUC and sSCUC approaches is relevant. Also, since
242 different TSOs use different scheduling timescales and/or different rolling ap-
243 proaches, e.g. every 15 minute [39], or every 5 minute [8], a comparison of the
244 effect of these strategies is also carried out in this section. Moreover, the im-
245 pact of contingency and renewable penetration on the transient response of the
246 system and long-term frequency deviations, respectively, using different sSCUC
247 strategies is shown as well. Finally, the impact of different wind power scenarios
248 of the sSCUC on the dynamic response of the system is discussed.

249 All simulations are based on a modified IEEE 39-bus system [40], with the
250 data of the sSCUC taken from [41]. Whereas the value of load curtailment is
251 assumed \$1000/MWh [4], and the marginal cost of wind is considered zero. The
252 focus is on the first 12 hours of the planning horizon. During these hours the
253 demand increases from 700 MW in the first hour to 1500 MW in the 12 hour. For
254 simplicity, a wind profile that follows the demand is modelled. In other words,
255 we assume the same wind penetration level for the medium scenario during
256 these hours, namely, 25%, and based on this we build the low and high scenario
257 accordingly. Such a relationship between demand and wind power corresponds
258 to a typical day in 2018 in the Irish system. It should be noted here that one
259 may choose any other profile for the demand and wind but according to our
260 studies that does not change the relevant conclusions. Wind generation is given
261 by three wind power plants connected at bus 20, 21 and 23, respectively, with
262 a nominal capacity of 300 MW each.

263 The total number of state and algebraic variables of the SDAE model for
264 all scenarios are 173 and 277, respectively. Regarding the sSCUC variables, the
265 model includes three first-stage variables, namely, the ON/OFF, start-up and

266 shut-down status of generating units, and four second-stage variables, namely,
267 the active power of conventional units (set-points), the demand and wind power
268 curtailment, and the bus voltage angle, respectively. The total numbers of
269 the first-stage and second-stage variables for the 15-minute model are 2,880
270 and 20,448, respectively. While the total numbers of these variables for the 5
271 minute model are 8,640 and 61,344, respectively. Therefore even considering
272 only three wind power scenarios, shortening the time period of sSCUC, lead
273 to a huge increase in the size of the sSCUC model. In fact, this is one of the
274 main limitations of sSCUC approaches, especially when considering their use
275 for real-time operations of power systems.

276 Finally, a Monte Carlo method is used in all scenarios (100 simulations are
277 solved for each scenario). The standard deviation of the frequency of the COI,
278 σ_{COI} , (computed as the average of the standard deviation obtained for each
279 trajectory) is utilized as an index to evaluate the impact of sSCUC on the
280 dynamic response of the system. The sSCUC is implemented in the Python
281 language and solved using Gurobi [42], while all simulations are obtained using
282 DOME, a Python-based software tool [37]. DOME includes a set of dynamic
283 models similar to the ones provided by commercial software tools but with
284 the additional feature of being able to model and properly integrate stochastic
285 processes.

286 *3.1. 15-Minute Scheduling*

287 In this case study, a 15-minute scheduling time period is used. The average
288 value of the objective function is found to be approximately \$412,000, hence,
289 lower than the value found in, for example, [41]. This is due to the fact that
290 wind generation is explicitly accounted in the objective function, and since its
291 marginal production cost is considered zero, it leads to lower operational costs.
292 Each scenario is characterized by a relevant amount of wind stochastic varia-
293 tions. When solving the sensitivity analysis, the sSCUC probabilities are varied,
294 and their impact on the standard deviation of the frequency of the system (σ_{COI})
295 is observed.

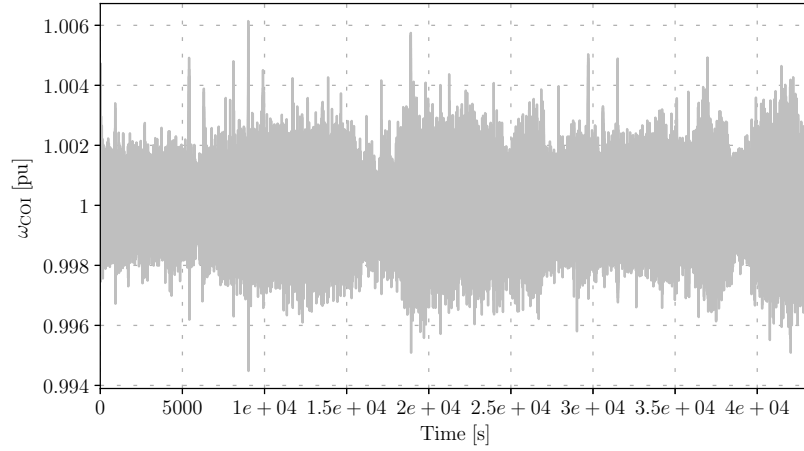


Figure 4: 15-minute scheduling – Trajectories of ω_{COI} for 12h.

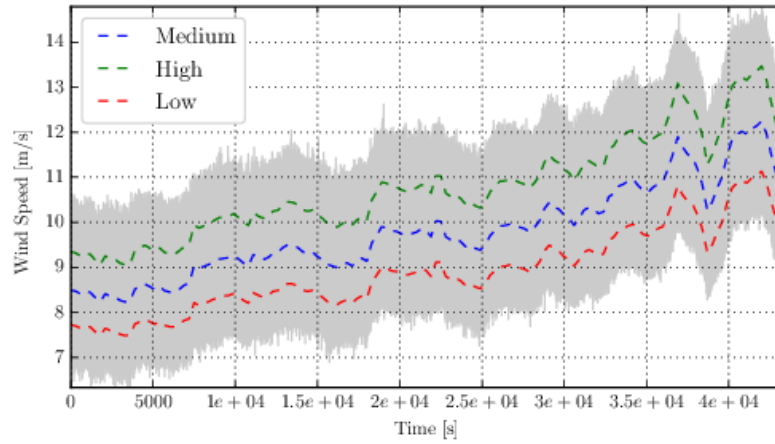


Figure 5: 15-minute scheduling – Trajectories of wind speeds for 12h. Dashed lines indicate the high, medium and low scenarios, respectively, while grey line indicate the same scenarios with inclusion of volatility.

296 In order to compare results, a base-case scenario is considered with the
 297 following properties: sSCUC probabilities for the low, medium and high wind
 298 power scenarios are set to 20%, 60%, 20%, respectively. Similarly, when we

299 run the Monte Carlo TDS (MC-TDS), the system is assumed to be with the
 300 following probabilities: 20%, 60%, 20% for the low, medium and high wind
 301 power scenario, respectively. As mentioned in the rolling planning section, the
 302 low and high scenario differ from the medium scenario by 10%. This base case
 303 is shown in Fig. 4, 5, while Fig. 4 shows the trajectories of ω_{COI} and Fig. 5
 304 shows the trajectories of the wind speed scenarios.

305 It is interesting to note that, in Fig. 4, the frequency jumps due to a change
 306 in the operating point of the machines forced by the sSCUC, i.e. new schedules.
 307 These jumps are very similar to real-world power systems behaviour observed
 308 in, for example, the continental European grid [24, 43]. Finally, it is worth
 309 mentioning that the wind speed profile in Fig. 5 is obtained by adding some
 310 stochastic noise on each of the three wind scenarios.

311 3.1.1. Impact of different sSCUC strategies on power system dynamics

312 Table 1 shows some of the most relevant results of the sensitivity analysis.
 313 Specifically, scenario 1 assumes a sSCUC with wind probabilities 20%, 60%,
 314 20% and a MC-TDS with the same probabilities. Thus, it is assumed that what
 315 was forecast by the sSCUC will actually happen in the reality. σ_{COI} for this
 316 scenario is 0.000847. In Scenario 2 the probabilities of the sSCUC differ from
 317 that of the system by a relevant value. The value of σ_{COI} is 0.000859, and thus
 318 higher than scenario 1 due to the error in the sSCUC probabilities.

319 Scenario 3 assumes a sSCUC with 100% low wind (one scenario, equivalent
 320 to SCUC). The value of σ_{COI} for this scenario is 0.000867 and so higher than
 321 scenario 1 for the same reason above. Similarly, Scenario 4 assumes a sSCUC
 322 with 100% medium wind. This leads to higher frequency variations compared
 323 to scenario 1, with $\sigma_{COI} = 0.000872$. Next, Scenario 5 assumes a sSCUC with
 324 100% high wind. Quite surprisingly this scenario appears to be the best from
 325 the dynamic point of view with $\sigma_{COI} = 0.000802$.

326 To analyse this relevant case, more scenarios are considered. In Scenarios
 327 6 to 9 in Table 1, the probabilities of sSCUC are varied from a sSCUC with
 328 100% high wind to a sSCUC with 100% medium, and it can be seen that σ_{COI}

Table 1: 15-minute scheduling – σ_{COI} for different sSCUC probabilities with $j = 10\%$.

Scenario	sSCUC	MC – TDS	$\sigma_{\text{COI}} (10^{-4})$
1	20% 60% 20%	20% 60% 20%	8.47
2	40% 50% 10%	20% 60% 20%	8.59
3	100% 0% 0%	20% 60% 20%	8.67
4	0% 100% 0%	20% 60% 20%	8.72
5	0% 0% 100%	20% 60% 20%	8.02
6	0% 20% 80%	20% 60% 20%	8.17
7	0% 40% 60%	20% 60% 20%	8.32
8	0% 60% 40%	20% 60% 20%	8.41
9	0% 80% 20%	20% 60% 20%	8.52

329 increases almost linearly. Therefore, even though Scenario 5 assumes an error
 330 in the sSCUC probabilities, synchronous machines and the respective controls
 331 (primary and secondary) can regulate it very fast.

332 To further analyse this, in Table 2 the wind power uncertainty level is in-
 333 creased from $j = 10\%$ to $j = 30\%$ with a step of 10% for both, Scenario 1
 334 and Scenario 5, respectively. For $j \geq 30\%$, Scenario 1 gives the better dynamic
 335 behaviour. It appears that, if the wind forecast error is small, then from the
 336 dynamic performance viewpoint of the system, it is better to solve a SCUC with
 337 high wind power.

338 It is worth observing that the differences on the long-term frequency devi-
 339 ations of the system between scenarios are marginal (maximum of 3.5 mHz).
 340 This is mainly due to the fact that, since the scheduling is repeated with a
 341 short period, it reduces the forecast error, which in turn leads different sSCUC
 342 strategies to produce similar schedules for the generators. This indicates that
 343 system operators may prefer to use deterministic approaches when scheduling

Table 2: 15-minute scheduling – σ_{COI} for different sSCUC probabilities and different j .

Scenario	j	sSCUC	MC – TDS	$\sigma_{\text{COI}} (10^{-4})$
1	10%	20% 60% 20%	20% 60% 20%	8.47
1	20%	20% 60% 20%	20% 60% 20%	12.58
1	30%	20% 60% 20%	20% 60% 20%	17.20
5	10%	0% 0% 100%	20% 60% 20%	8.02
5	20%	0% 0% 100%	20% 60% 20%	12.41
5	30%	0% 0% 100%	20% 60% 20%	17.37

Table 3: 15-minute scheduling – σ_{COI} for different sSCUC probabilities with $j = 10\%$.

Scenario	sSCUC	MC – TDS	$\sigma_{\text{COI}} (10^{-4})$
1	0% 0% 100%	0% 0% 100%	8.01
2	0% 100% 0%	0% 100% 0%	2.90
3	100% 0% 0%	100% 0% 0%	1.46

344 the system as the complexity of the stochastic one does not provide a solution
 345 with a significant added value for the operation of the system.

346 Finally, Table 3 compares three deterministic cases, namely, low, medium
 347 and high sSCUC wind power scenarios. The deterministic low wind power
 348 scenario leads to better dynamic behaviour (lower σ_{COI}).

349 3.1.2. Impact of sSCUC wind uncertainty on power system dynamics

350 To simulate the impact of the sSCUC wind power uncertainty, the uncer-
 351 tainty level is increased from $j = 10\%$ to $j = 40\%$ with a step of 10% (volatility
 352 is kept constant). Four σ_{COI} are calculated and Fig. 6 shows σ_{COI} as a function
 353 of wind power uncertainty. The higher wind uncertainty, the higher σ_{COI} . This
 354 relationship is almost linear within the used range. This suggests that as power

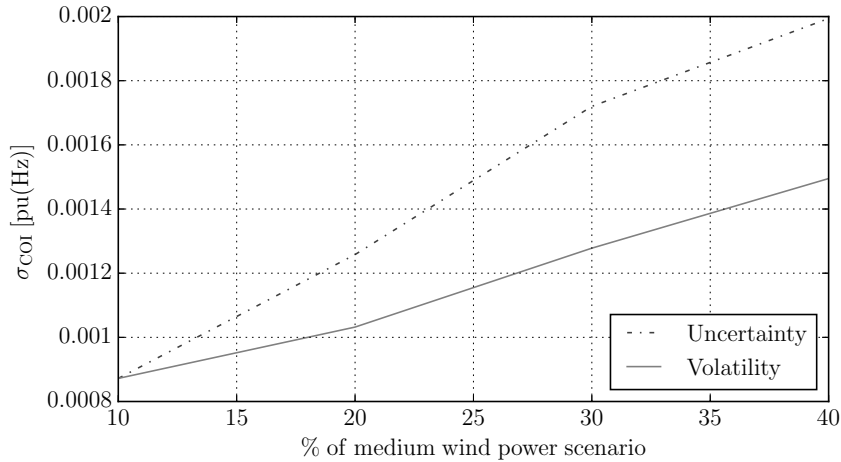


Figure 6: 15-minute scheduling – σ_{COI} as a function of wind uncertainty and volatility.

355 systems accommodate larger amounts of RES, i.e. higher uncertainty, TSOs will
 356 have to make sure that they have the necessary sources (power reserve) to cope
 357 with this uncertainty.

358 Figure 7 shows the total cost as a function of wind uncertainty. The higher
 359 the wind uncertainty, the higher the cost due to more ramp-up and ramp-
 360 down of generators. Hence, despite RES being a cheap source of energy, their
 361 intermittent nature, requires more reserves to cope and so there will be an
 362 increase of the cost of ancillary service. These results confirm the conclusions
 363 of previous works, e.g. [34].

364 3.1.3. Impact of sSCUC wind volatility on power system dynamics

365 To study the impact of sSCUC wind power volatility on power system dy-
 366 namics, different level of volatility are considered, i.e., higher standard devi-
 367 ations means high wind volatility. The standard deviation of wind scenarios
 368 is increased from 10% to 40% with a step of 10% while uncertainty is kept
 369 constant.

370 Figure 6 shows σ_{COI} as a function of wind power standard deviation. The
 371 higher the wind power volatility, the higher the frequency variations. Similarly

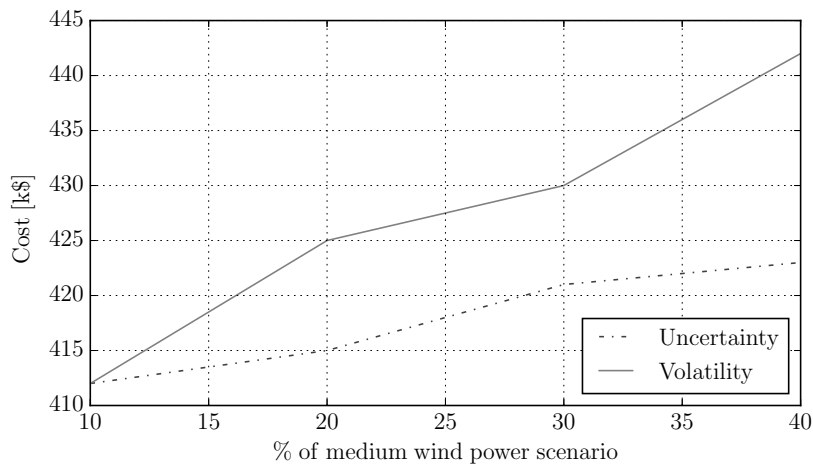


Figure 7: 15-minute scheduling – Expected cost as a function of wind uncertainty and volatility.

372 to the results shown in Fig. 6, this relationship appears to be almost linear
 373 within the considered range. As mentioned above, this supports the idea for
 374 increased ancillary services by TSOs in the future.

375 Figure 7 shows the total cost as a function of wind volatility where it can
 376 be seen that higher wind power volatility leads to higher costs due to higher
 377 ramping of generating units. Wind power volatility has thus a greater impact
 378 than uncertainty on costs.

379 3.2. 5-Minute Scheduling

380 In this scenario, the wind power uncertainty level is assumed proportional
 381 lower compared to the 15-minute scheduling time period ($j = 3.33\%$). This
 382 assumption is made based on the 15-minute rate of change of wind power shown
 383 above (Fig. 1). Next, the base case scenario is depicted in Fig. 8, 9. Compared to
 384 the base-case scenario in the 15-minute case study (Fig. 4), frequency variations
 385 are lower (Fig. 8). Also, it is interesting to note that high frequency variations
 386 correspond to the wind ramp-up. Regarding the total operating cost, its average
 387 value is found to be approximately \$408,000, and hence, lower than in 15-minute
 388 case study due to lower uncertainty.

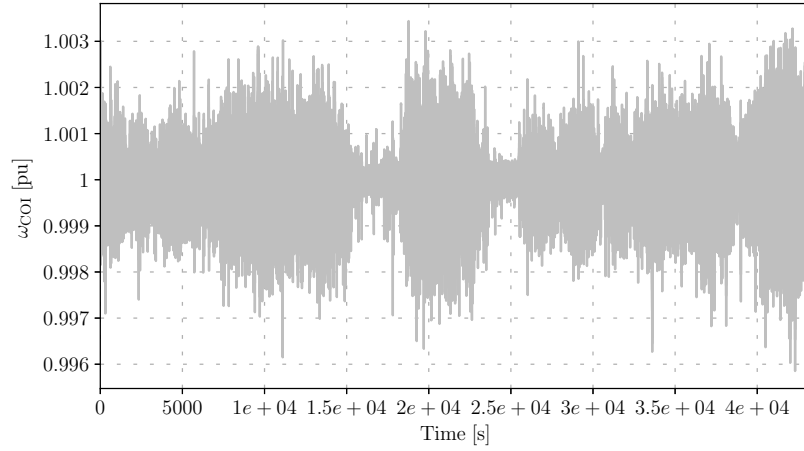


Figure 8: 5-minute scheduling – Trajectories of ω_{COI} for 12h.

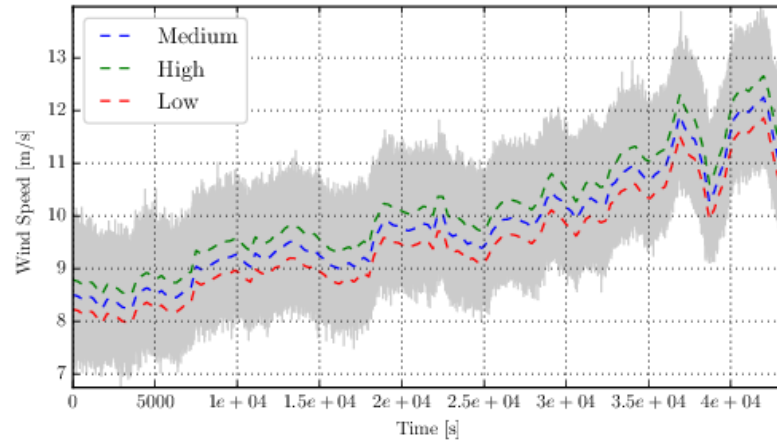


Figure 9: 5-minute scheduling – Trajectories of wind speeds for 12h. Dashed lines indicate the high, medium and low scenarios, respectively, while grey line indicate the same scenarios with inclusion of volatility.

389 *3.2.1. Impact of different sSCUC strategies on power system dynamics*

390 This section perform the same sensitivity analysis that is carried out for the
 391 15-minute scheduling. Table 4 show the relevant results of such an analysis. A

Table 4: 5-minute scheduling – σ_{COI} for different sSCUC probabilities with $j = 3.333\%$.

Scenario	sSCUC	MC – TDS	$\sigma_{\text{COI}} (10^{-4})$
1	20% 60% 20%	20% 60% 20%	5.45
2	40% 50% 10%	20% 60% 20%	5.51
3	100% 0% 0%	20% 60% 20%	5.44
4	0% 100% 0%	20% 60% 20%	5.70
5	0% 0% 100%	20% 60% 20%	5.48
6	0% 20% 80%	20% 60% 20%	5.53
7	0% 40% 60%	20% 60% 20%	5.55
8	0% 60% 40%	20% 60% 20%	5.55
9	0% 80% 20%	20% 60% 20%	5.59

392 reduction of the value of σ_{COI} is observed for all scenarios. This is due to the
393 lower level of wind power uncertainty. In particular, if we compare scenarios 1, 3
394 and 5, respectively, we can see that the differences are less significant. It appears
395 that, if the uncertainty level is low and the system is scheduled more frequently,
396 then differences between SCUC and sSCUC becomes less evident. This result
397 can be explained by the fact that, even if there is an error in the forecast, the
398 machines and the relevant controls will easily account for it. Therefore, if shorter
399 interval of sSCUC are used and the system is scheduled more frequently, like, for
400 example, in Australia [8], then system operators can still rely on deterministic
401 approaches without compromising the dynamic performance of the system.

402 While the sensitivity analysis in case of the perfect forecast is shown in Table
403 5. The deterministic case with low wind gives the better dynamic behaviour,
404 thus confirming the conclusions drawn for the 15-minute sSCUC.

Table 5: 5-minute scheduling – σ_{COI} for different sSCUC probabilities with $j = 3.333\%$.

Scenario	sSCUC	MC – TDS	σ_{COI} (10^{-4})
1	0% 0% 100%	0% 0% 100%	5.46
2	0% 100% 0%	0% 100% 0%	3.38
3	100% 0% 0%	100% 0% 0%	2.43

405 *3.2.2. Impact of sSCUC wind uncertainty on power system dynamics*

406 This section focus on the impact of wind power uncertainty on power system
 407 dynamics using a 5-minute scheduling. Similar to the 15-minute case, the wind
 408 power uncertainty level is increased from $j = 10\%$ to $j = 40\%$ with a step of
 409 10% .

410 Figure 10 shows σ_{COI} as a function of wind power uncertainty. Again, we
 411 can see that such a relationship is almost linear within the used range. This
 412 suggests that, even using shorter sSCUC timescales, e.g. 5 minute, higher shares
 413 of RES will likely affect the dynamic performance of the system.

414 *3.2.3. Impact of sSCUC wind volatility on power system dynamics*

415 Following the same procedure as in the 15-minute case study, the standard
 416 deviation of wind power scenarios is increased from 10% to 40% with a step of
 417 10% . Then, Fig. 10 shows σ_{COI} as a function of wind power volatility. This
 418 relationship is almost linear within the considered range, and so these findings
 419 just support the conclusions made above. Finally, the impact of wind power
 420 volatility on costs is shown in Fig. 11. Results indicate that the higher the wind
 421 power volatility, the higher the cost due to more ramping of generating units.

422 *3.3. Impact of contingency on the transient response of the system using sSCUC
 423 and SCUC*

424 In this section, we discuss whether a contingency leads to different dynamic
 425 behaviour of the system if using a sSCUC or SCUC. With this aim, the com-

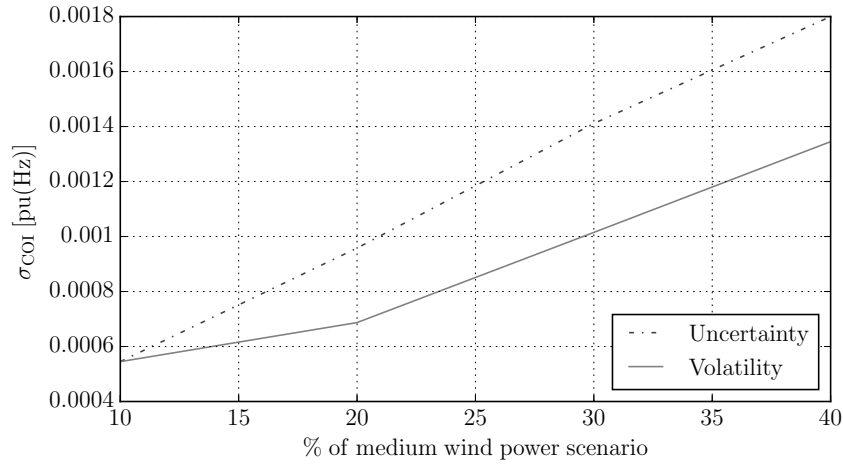


Figure 10: 5-minute scheduling – σ_{COI} as a function of wind uncertainty and volatility.

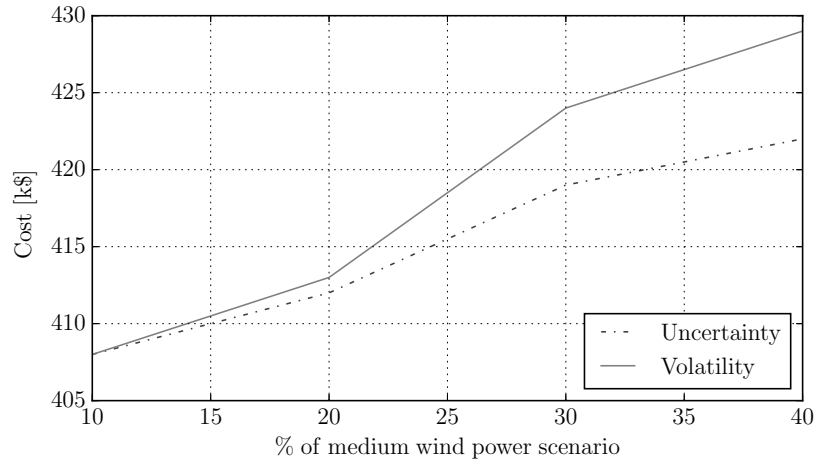


Figure 11: 5-min scheduling – Expected cost as a function of wind uncertainty and volatility.

426 parison is performed using scenario 1 (stochastic) and scenario 5 (deterministic)
 427 from Table 1.

428 A three-phase fault is applied at $t = 900$ s and cleared after 200 ms by
 429 disconnecting line 1. The impact of the contingency is shown in Figs. 12 and
 430 13. Specifically, Fig. 12 depicts the trajectories of the rotor speed of the rele-
 431 vant machines during the contingency when using a sSCUC. Similarly, Fig. 13

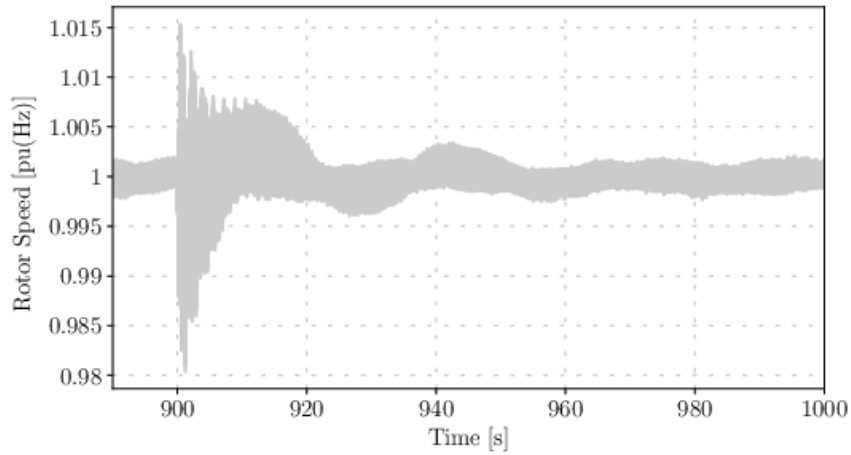


Figure 12: sSCUC and 25% wind penetration – Trajectories of the rotor speed of relevant machines following a contingency.

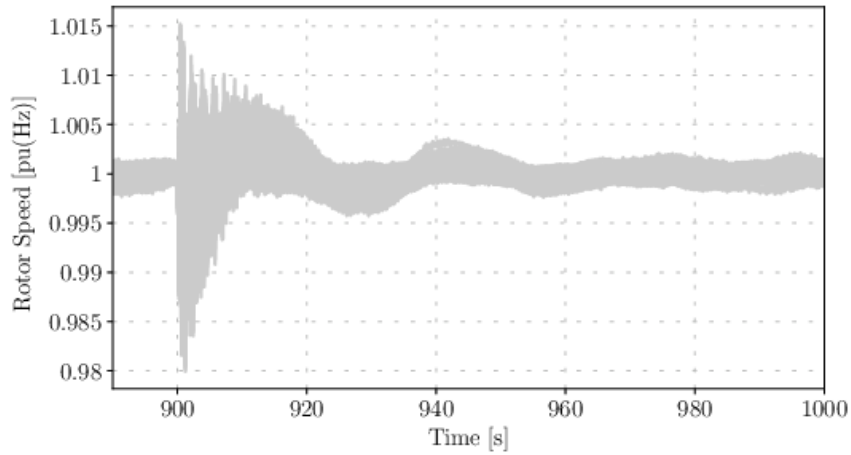


Figure 13: SCUC and 25% wind penetration – Trajectories of the rotor speed of relevant machines following a contingency.

432 depicts the trajectories of the rotor speed of the relevant machines during the
 433 contingency when using a SCUC. Results indicate that for the considered case
 434 study the impact of contingency is almost identical. This is due to the fact
 435 that the generator schedules obtained with the sSCUC and SCUC do not differ

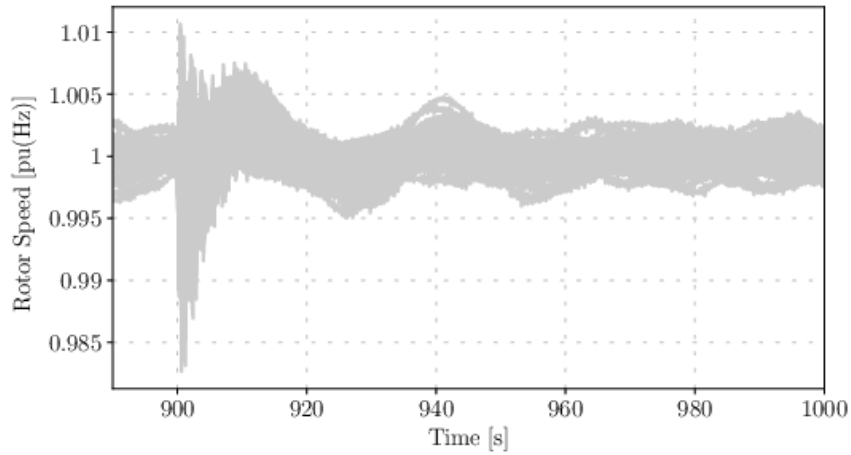


Figure 14: sSCUC and 50% wind penetration – Trajectories of the rotor speed of relevant machines following a contingency.

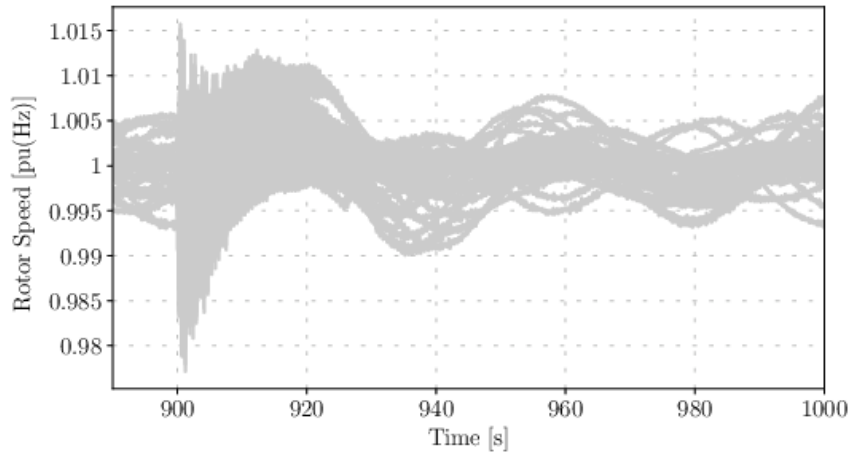


Figure 15: SCUC and 50% wind penetration – Trajectories of the rotor speed of relevant machines following a contingency.

436 significantly.

437 The same contingency is applied for the case of 50% wind penetration. Fig-
 438 ures 14 and 15 show the trajectories of the rotor speed of the relevant machines
 439 during the contingency when using a sSCUC and SCUC, respectively. In this

440 case, the sSCUC leads to a better transient response of the system following
441 a contingency. It appears that, one cannot know *a priori* which strategies of
442 sSCUC are better from the dynamic viewpoint of the system before solving both
443 sSCUC and SCUC problems.

444 *3.4. Impact of renewable penetration on long-term frequency deviations using* 445 *different sSCUC strategies*

446 Increasing the penetration levels of RES changes the stability and dynamic
447 performance of the system as well as makes real-time system operation more
448 difficult for TSOs [2]. In this context, this section focuses on the impact of high
449 penetration levels of RES, namely 50%, on the long-term frequency deviations
450 using different sSCUC strategies. With this aim, and similar to Subsection 3.1.1,
451 a sensitivity analysis with respect to different sSCUC probabilities for the low,
452 medium and high wind power scenario is carried out.

453 Table 6 shows some relevant results of the analysis. There is a significant
454 increase in the value of σ_{COI} in all scenarios compared to the case of 25% of
455 wind penetration. This is to be expected as fewer synchronous generators that
456 provide frequency regulation (primary and secondary) are now scheduled to be
457 online and more power is being produced by stochastic sources.

458 It is interesting to note that the deterministic scenario with high wind power
459 (scenario 5) is the worst with $\sigma_{\text{COI}} = 0.002618$. Scenario 5, in fact, schedules
460 fewer synchronous generators to be online compared to the same scenario in
461 Section 3.1.1. In other words, there is less frequency regulation available online
462 to cope with wind power uncertainty. Therefore, depending on the level of wind
463 power uncertainty, as well as wind penetration level, TSOs can solve a sSCUC
464 or SCUC with high wind. Specifically, according to our results, for low wind
465 power uncertainty ($j < 30\%$) and 25% wind penetration level, it is better to
466 solve a SCUC with high wind power. On the other hand, if the wind penetration
467 level is 50% then TSOs can solve a sSCUC and/or SCUC with medium and low
468 wind power, respectively.

Table 6: 15-minute scheduling – σ_{COI} for different sSCUC probabilities with $j = 10\%$ and 50% wind penetration.

Scenario	sSCUC	MC – TDS	$\sigma_{\text{COI}} (10^{-4})$
1	20% 60% 20%	20% 60% 20%	19.03
2	40% 50% 10%	20% 60% 20%	18.95
3	100% 0% 0%	20% 60% 20%	19.09
4	0% 100% 0%	20% 60% 20%	19.09
5	0% 0% 100%	20% 60% 20%	26.18

469 *3.5. Impact of the number of sSCUC wind scenarios on the dynamic response*
 470 *of the system*

471 In this section, we compare the impact of the number of sSCUC wind scenar-
 472 ios on the dynamic behaviour of power system. The comparison is performed
 473 using a 15 minute scheduling time period and 25% wind penetration. With this
 474 aim, we consider 10 wind power scenarios and perform a sensitivity analysis
 475 similar to Subsection 3.1.1. Wind power scenarios are built according to the
 476 wind maximum variation width j (see Fig. 1). In order to compare the results,
 477 a base-case scenario is considered with the following properties: sSCUC proba-
 478 bilities for the 10 scenarios (starting from low to high wind) are set as follows:
 479 5%, 5%, 10%, 10%, 30%, 10%, 10%, 10%, 5%, 5%. Similarly, when we run
 480 the MC-TDS, the system is assumed to be with the following probabilities: 5%,
 481 5%, 10%, 10%, 30%, 10%, 10%, 10%, 5%, 5%, starting from low to high wind
 482 scenario, respectively.

483 Figure 16 shows the trajectories of ω_{COI} for this base case scenario. Com-
 484 pared to Fig. 4 (3 sSCUC wind power scenarios), there is no significant difference
 485 in the dynamic behaviour of the system. To further support this, Table 7 shows
 486 some of the relevant results of the sensitivity analysis. As it can be seen, the
 487 long-term frequency deviations are similar to those in Table 1 and do not differ

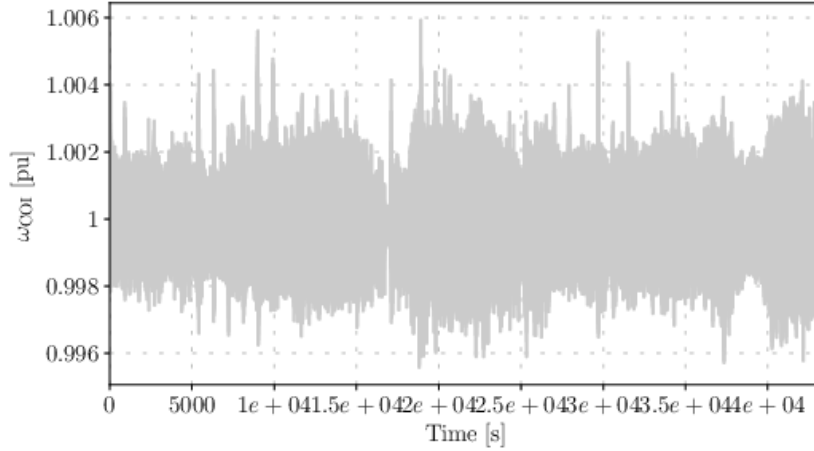


Figure 16: 15-minute scheduling – Trajectories of ω_{COI} for 10 sSCUC wind power scenarios.

Table 7: 15-minute scheduling – σ_{COI} for different sSCUC probabilities with $j = 10\%$ and 10 wind power scenarios.

Scenario	sSCUC	MC – TDS	$\sigma_{\text{COI}} (10^{-4})$
1	5%, 5%, 10%, 10%, 30%, 10%, 10%, 10%, 5%, 5%	5%, 5%, 10%, 10%, 30%, 10%, 10%, 10%, 5%, 5%	8.74
2	20%, 5%, 5%, 10%, 10%, 5%, 10%, 10%, 5%, 20%	5%, 5%, 10%, 10%, 30%, 10%, 10%, 10%, 5%, 5%	8.77
3	100%, 0%, 0%, 0%, 0%, 0%, 0%, 0%, 0%, 0%	5%, 5%, 10%, 10%, 30%, 10%, 10%, 10%, 5%, 5%	8.82
4	0%, 0%, 0%, 0%, 100%, 0%, 0%, 0%, 0%, 0%	5%, 5%, 10%, 10%, 30%, 10%, 10%, 10%, 5%, 5%	8.99
5	0%, 0%, 0%, 0%, 0%, 0%, 0%, 0%, 0%, 100%	5%, 5%, 10%, 10%, 30%, 10%, 10%, 10%, 5%, 5%	8.90

488 significantly between scenarios. It appears that, for the considered case, increas-
 489 ing the number of sSCUC wind power scenarios from 3 to 10 does not have a
 490 significant impact on the dynamic response of the system. Furthermore, these
 491 results support the above conclusion that a highly sophisticated sSCUC might
 492 not be necessary if the scheduling is repeated with a short period.

493 3.6. Remarks and Recommendations

494 The results obtained in the case studies can be grouped in two categories,
 495 namely, as expected and less expected.

496 *3.6.1. As expected*

- 497 • Simulation results show that there exist a relationship between sSCUC in-
498 tervals and frequency deviations. Shortening the sSCUC interval, e.g. from
499 15 to 5 minutes, leads to lower frequency fluctuations. These findings are
500 in line with the results that were observed in real-world power systems
501 [43].
- 502 • In case of perfect forecasts, simulation results show that the scenario with
503 low wind gives a better dynamic behaviour compared to the medium and
504 high wind power scenario.
- 505 • All simulation results show an almost linear relationship between sSCUC
506 wind uncertainty and volatility and frequency variations. This means that
507 as the penetration of RES increases, i.e., higher wind uncertainty and
508 volatility, it will be more and more difficult for TSOs to manage the real-
509 time balance between generation and demand. Therefore, there is a clear
510 need for linear increase of the spinning reserves. Actually, these results
511 support the idea that in systems with high RES penetration, e.g. Denmark
512 and Ireland, the main concern for TSOs will be on how to cope with
513 high ramp-up and ramp-down of RES rather than the traditional $N - 1$
514 contingency criteria.
- 515 • In general, higher RES penetration leads to lower costs. However, simu-
516 lation results indicate that while the total operating cost will be reduced,
517 the reward of ancillary services will increase due to more ramping of gen-
518 erating units.
- 519 • Increasing the number of sSCUC wind power scenarios, namely, from 3 to
520 10, leads to very similar long-term frequency deviations of the system.

521 *3.6.2. Less expected*

- 522 • Different sSCUC strategies leads to very similar long-term dynamic be-
523 haviour of the system.

- 524 • For low wind uncertainty ($j < 30\%$) and 25% wind penetration level,
525 solving a SCUC with high wind gives a better dynamic behaviour. Never-
526 theless, as uncertainty increases, it is recommended that a sSCUC should
527 be used. When the wind penetration level is 50% then it is better to
528 solve a sSCUC and/or SCUC with medium and low wind power, respec-
529 tively. Moreover, when shortening the sSCUC interval and scheduling
530 the system more frequently, the differences between these strategies are
531 negligible. This is an important information for system operators since
532 they still rely on deterministic approaches. Therefore, depending on the
533 level of wind penetration and uncertainty, they can solve a SCUC without
534 compromising the dynamic behaviour of power systems.
- 535 • According to our results, in case of 25% wind penetration, there is no
536 significant difference on the transient response of the system following a
537 contingency when using a sSCUC or SCUC. However, when increasing
538 the wind penetration to 50% then a sSCUC leads to a better transient
539 response of the system. Note that the 50% penetration is not a fixed
540 threshold but depends on the considered grid, generator bids and available
541 wind generation.
- 542 • Finally, results show that wind power uncertainty has a greater impact
543 than volatility on the dynamic performance of the system, while the other
544 way round is true for the impact on the expected cost.

545 4. Conclusions

546 This paper analyses the impact of the sub-hourly UC problem on power
547 system dynamics. More specifically, the paper focuses on the impact of different
548 strategies of sSCUC as well as different wind uncertainty and volatility scenarios
549 included in the sSCUC on frequency variations. With this aim, a sub-hourly
550 sSCUC is used to capture wind variability, while the uncertainty is captured
551 through a stochastic sSCUC. Then, the sub-hourly sSCUC is embedded into a

552 time domain simulator (TDS), and a rolling approach is used to account for wind
553 and load forecast updates. Embedding the UC problem into a TDS provides an
554 useful simulation tool for TSOs in order to understand the impact interactions
555 of UCs models with the actual dynamic response of the grid.

556 Simulation results based on MC-TDS show that there is no significant dif-
557 ference on long-term frequency deviations of the system when using different
558 sSCUC strategies. Results also suggest that for low wind uncertainty, and 25%
559 wind penetration level, system operators may want to solve a SCUC with high
560 wind. However, as the sSCUC wind uncertainty increases then a sSCUC ap-
561 proach is to be preferred. In addition, in case the system is scheduled more
562 frequently, then differences between stochastic and deterministic approaches
563 becomes less evident. Regarding the impact of sSCUC wind scenarios, the case
564 study shows that, increasing the number scenarios does not lead to any sig-
565 nificant difference in the long-term frequency deviations. Furthermore, results
566 show that sSCUC wind power uncertainty has a greater impact than volatility
567 on the dynamic behaviour of the system.

568 The case studies show an almost linear relationship between higher sSCUC
569 wind uncertainty and volatility, and higher frequency variations. From a TSO
570 point of view, this means a challenge for future operation as the penetration of
571 RES is expected to increase. Hence, the safe integration of RES indicate a need
572 for linear increased ancillary services (spinning reserves) in order to ensure a
573 reliable operation of power systems.

574 Results suggest that for 25% wind penetration, both sSCUC and SCUC leads
575 to almost identical transient response of the system following a contingency. On
576 one hand, sSCUC leads to a better transient response of the system in case of
577 50% wind penetration. On the other hand, when the wind penetration level
578 reaches 50%, solving a sSCUC and/or SCUC with medium and low wind power,
579 respectively, leads to lower long-term frequency deviations of the system.

580 Future work will focus on designing a feedback control that will take a signal
581 from the system and send it to the sSCUC. Other works will also consider the
582 interaction between sSCUC, microgrids and DAEs. Finally, a study on the

583 impact of sub-hourly UC with inclusion of voltage constraints on long-term
584 dynamic behaviour of the system will be considered.

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